

LEGEND

- Certified Milepost - Tenths
- Certified Milepost
- Preferred Alternative Milepost - Tenths
- Preferred Alternative Milepost
- Terrestrial Route HVDC
- Submarine Route HVDC
- Terrestrial Route HVAC
- Preliminary HDD Locations
- Preliminary Pipe Bridge Location
- 2021 Boring Location
- Previous (2013) Boring Location
- Streams/Ditches
- Railroad ROW
- Deviation Zone
- Deviation Zone Outside ROW
- Preferred Alternative Deviation Zone
- Preferred Alternative Deviation Zone Outside ROW
- Town Boundary
- Village Boundary
- State Park (OPRHP)

Parcel Ownership

TOWN NAME

Road Name

Village Name

Transmission Developers Inc.

Champlain Hudson Power Express Project

Champlain Hudson Power Express Inc.

BORING LOCATION PLAN

Selkirk to Catskill

Figure A-10

Sheet 17 of 18

Prepared by: **AECOM**

5/19/2021



TEST BORING LOG

PROJECT: TDI CHAMPLAIN HUDSON POWER EXPRESS

LOCATION: CSX RAILROAD ROW, NY

BORING B219.5-1

G.S. ELEV. N/A

FILE 195651

SHEET 1 OF 1

GROUNDWATER DATA

FIRST ENCOUNTERED 13.5'			
DEPTH	HOUR	DATE	ELAPSED TIME

METHOD OF ADVANCING BOREHOLE

a	FROM	0.0'	TO	10.0'
d	FROM	10.0'	TO	25.0'

DRILLER	R. CARUSO
HELPER	C. SMART
INSPECTOR	C. POPPE
DATE STARTED	12/05/2012
DATE COMPLETED	12/05/2012

DEPTH	A	B	C	DESCRIPTION	Wn	REMARKS
				BLACK M/C SANDY F/C GRAVEL-SIZED ROCK FRAGMENTS (FILL)		
	S-1	8 7 6 8		2.0		
				DARK BROWN M/F/C SAND, SM SILT, SM F/ GRAVEL (FILL)	9.1	
	S-2	5 17 9 9		4.0		
5	S-3	9 50/0.4		BROWN SILT, SM F/M SAND, TR F/ GRAVEL (FILL)	11.8	
				6.0		
	S-4	6 7 9 13		DARK BROWN TO BLACK SILTY C/F GRAVEL, SM M/F/C SAND (FILL)		
10	S-5	5 8 6 13		10.0	14.9	
15	S-6	11 17 17			31.2	WATER TABLE DETERMINED FROM WETNESS OF SAMPLE
				LIGHT BROWN TO BROWN CLAY, TR TO SM SILT, TR F/M SAND		
20	S-7	7 7 7			28.3	
				23.5		
25	S-8	1 2 1		GRAY SILT (THIXOTROPIC)		
				25.0		
				END OF BORING AT 25'		
30						
35						

NEW PROJECTS TEST BORING LOG 195651_TDI_CSX.GPJ SITE BLAUVELT.GDT 3/12/13

DRN.	TBT
CKD.	PWK

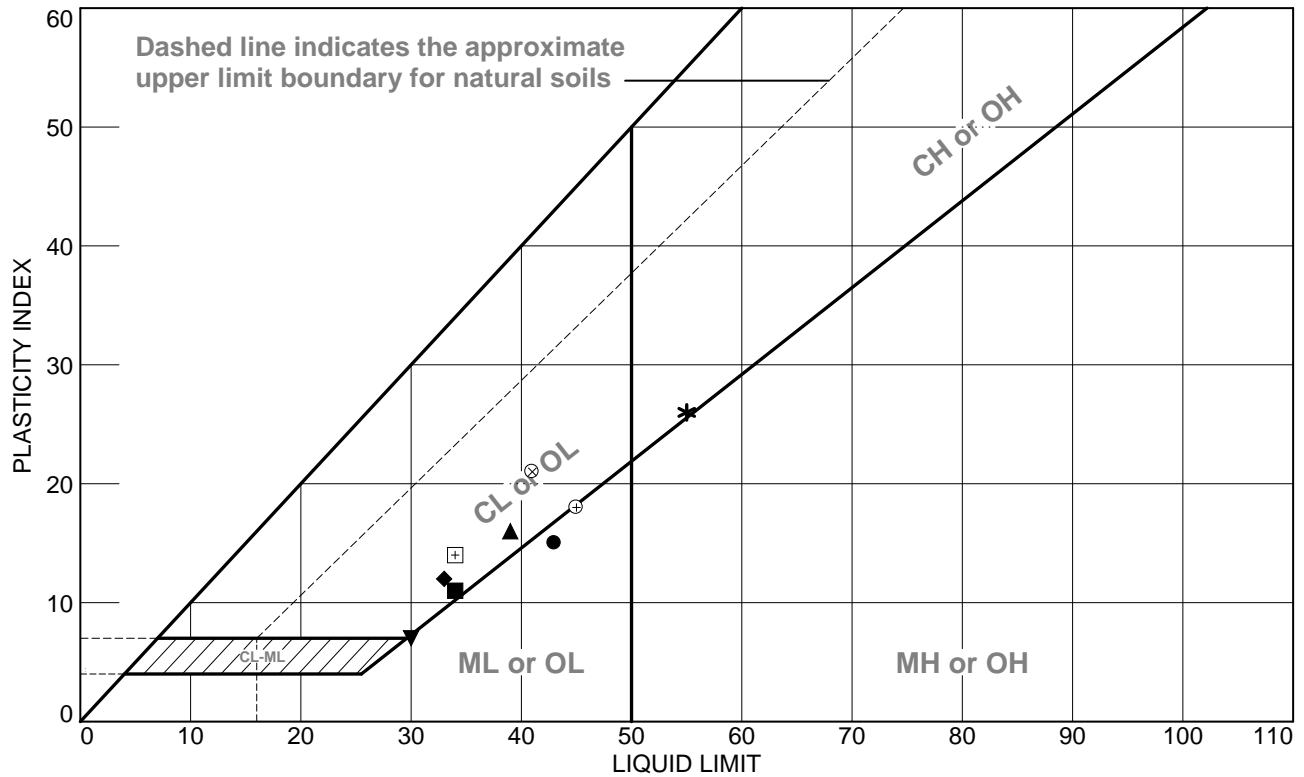


SUMMARY OF LABORATORY TEST DATA

Project Name: TDI Champlain Hudson Power Express – CSX
 Client Name: Transmission Developers, Inc.
 TRC Project #: 195651

SAMPLE IDENTIFICATION			Soil Group (USCS System)	GRAIN SIZE DISTRIBUTION				PLASTICITY				Specific Gravity	Moisture Content (%)	Unit Weight (pcf)	Compressive Strength (tsf)	Organic Content (%)
Boring #	Sample #	Depth (ft)		Gravel (%)	Sand (%)	Silt (%)	Clay (%)	Liquid Limit (%)	Plastic Limit (%)	Plasticity Index (%)	Liquidity Index					
	S-5	8.0-10.0	CH/MH					56	30	26	0.0	-	30.2	-	-	-
	S-6	13.5-15.0	ML	-	-	-	-	43	28	15	0.5	-	36.0	99.3	-	-
B219.5-1	S-2	2.0-4.0	SM	16.3	62.2	21.5		-	-	-	-	-	9.1	-	-	-
	S-3	4.0-4.9	-	-	-	-	-	-	-	-	-	-	11.8	-	-	-
	S-4	6.0-8.0	GM	35.2	25.6	39.2		-	-	-	-	-	14.9	-	-	-
	S-5	8.0-10.0														
	S-6	13.5-15.0	-	0.0	3.0	14.2	82.8	-	-	-	-	2.83	31.2	99.9	-	-
	S-7	18.5-20.0	CL					34	23	11	0.5	-	28.3	-	-	-
B220.3-1	S-2	2.0-4.0	-	-	-	-	-	-	-	-	-	-	48.8	-	-	10.7
	S-3	4.0-6.0	-	-	-	-	-	-	-	-	-	-	24.0	103.8	-	-
	S-5	8.0-10.0	-	0.0	4.9	23.5	71.5	-	-	-	-	2.80	27.6	-	-	-

LIQUID AND PLASTIC LIMITS TEST REPORT



SOIL DATA

	SOURCE	SAMPLE NO.	DEPTH	NATURAL WATER CONTENT (%)	PLASTIC LIMIT (%)	LIQUID LIMIT (%)	PLASTICITY INDEX (%)	USCS
●	A219.05-1	S-6	13.5-15.0 FT	36.0	28	43	15	ML
■	B219.5-1	S-7	18.5-20.0 FT	28.3	23	34	11	CL
▲	B220.3-1	S-6	13.5-15.0 FT	34.8	23	39	16	CL
◆	B220.3-1	S-7 & S-8	18.5-25.0 FT	26.9	21	33	12	CL
▼	B220.7-1	S-4 & S-5	6.0-10.0 FT	15.4	23	30	7	ML
*	B221.5-1	S-4 & S-5	6.0-10.0 FT	34.3	29	55	26	CH
⊕	B221.5-1	S-9	28.5-30.0 FT	38.2	27	45	18	CL/ML
⊕	B221.6-1	S-3, S-4, & S-5	4.0-10.0 FT	38.8	20	34	14	CL
⊗	B221.8-1	S-5	8.0-10.0 FT	40.2	20	41	21	CL

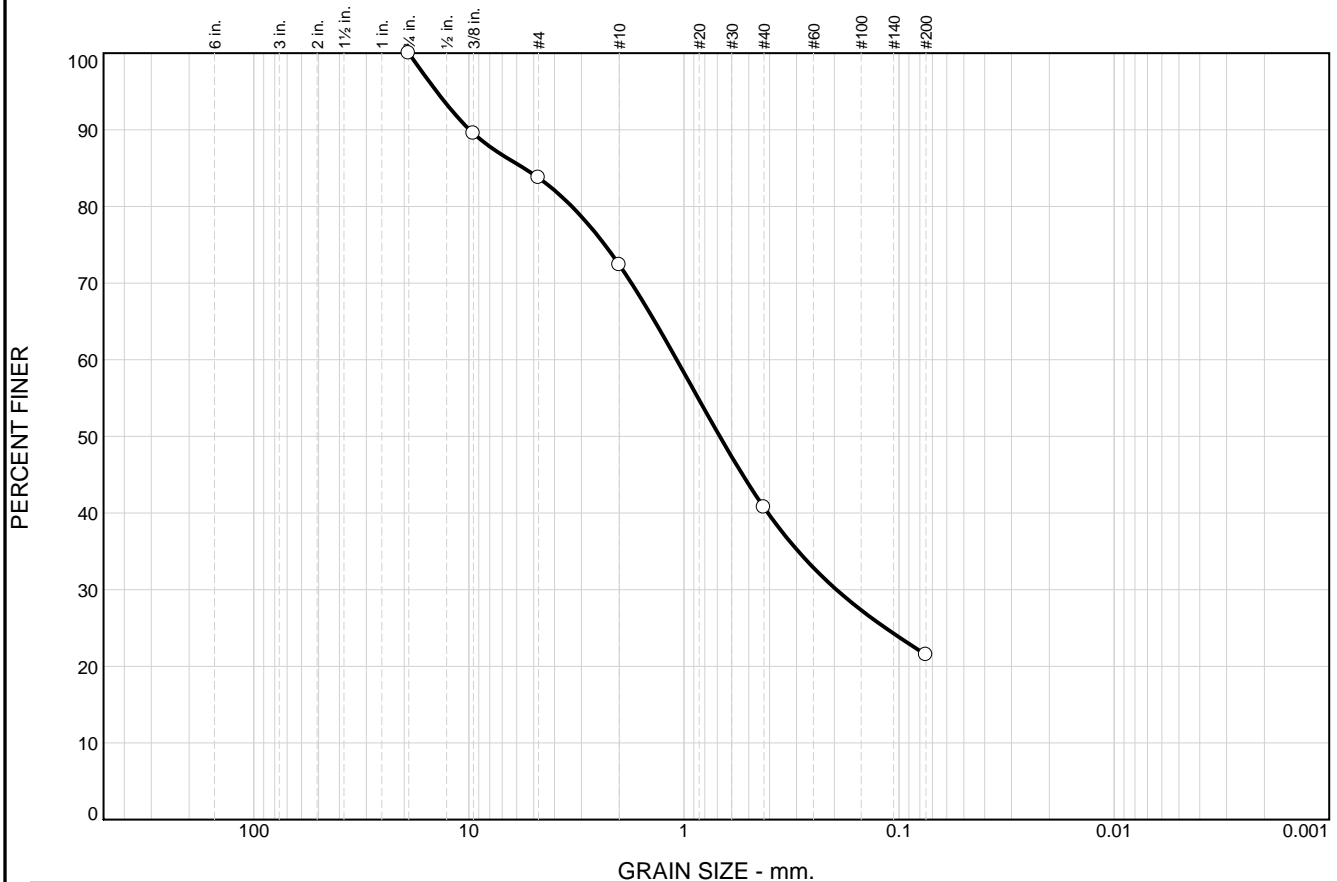
TRC
Engineers, Inc.
Mt. Laurel, NJ

Client: TRANSMISSION DEVELOPERS INC.
Project: TDI CHAMPLAIN HUDSON POWER EXPRESS - CSX

Project No.: 195651

Figure 8

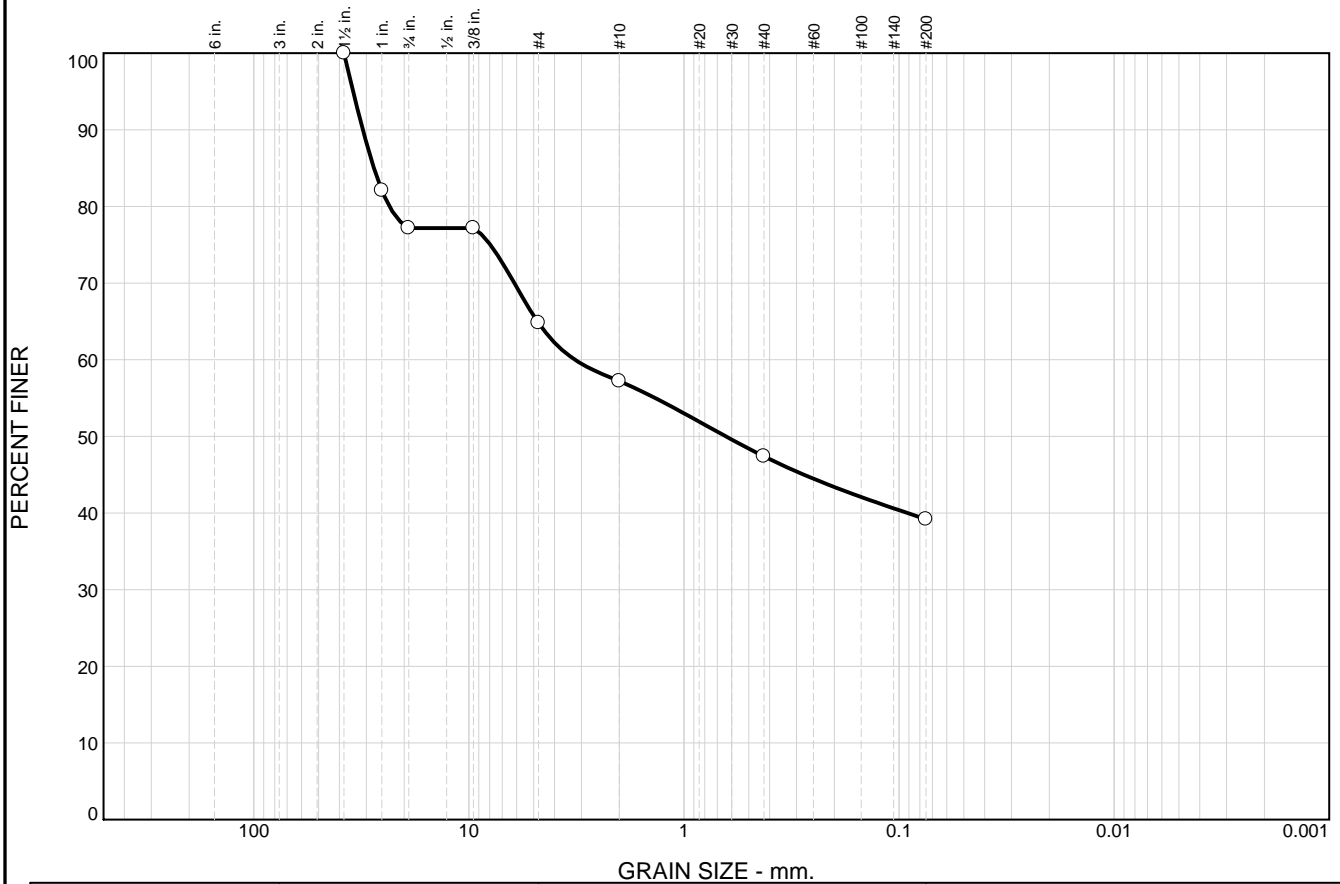
Particle Size Distribution Report



GRAIN SIZE - mm.											
% +3"		% Gravel		% Sand			% Fines				
		Coarse	Fine	Coarse	Medium	Fine	Silt		Clay		
○	0.0		0.0	16.3	11.3	31.7	19.2	21.5			
×	LL	PL	D ₈₅	D ₆₀	D ₅₀	D ₃₀	D ₁₅	D ₁₀	C _c	C _u	
○			5.5542	1.0811	0.6815	0.1955					
Material Description								USCS		AASHTO	
○ DARK BROWN M/F/C SAND, SM SILT, SM F/ GRAVEL								SM			
Project No. 195651 Client: TRANSMISSION DEVELOPERS INC. Project: TDI CHAMPLAIN HUDSON POWER EXPRESS - CSX								Remarks: ○SAMPLE DESCRIPTION BASED ON VISUAL IDENTIFICATION AND LABORATORY ANALYSIS			
○ Source of Sample: B219.5-1 Depth: 2.0-4.0 FT Sample Number: S-2											
TRC Engineers, Inc.								Figure 110			
Mt. Laurel, NJ											

Tested By: TBT 01/10/13 Checked By: JPB 03/12/13

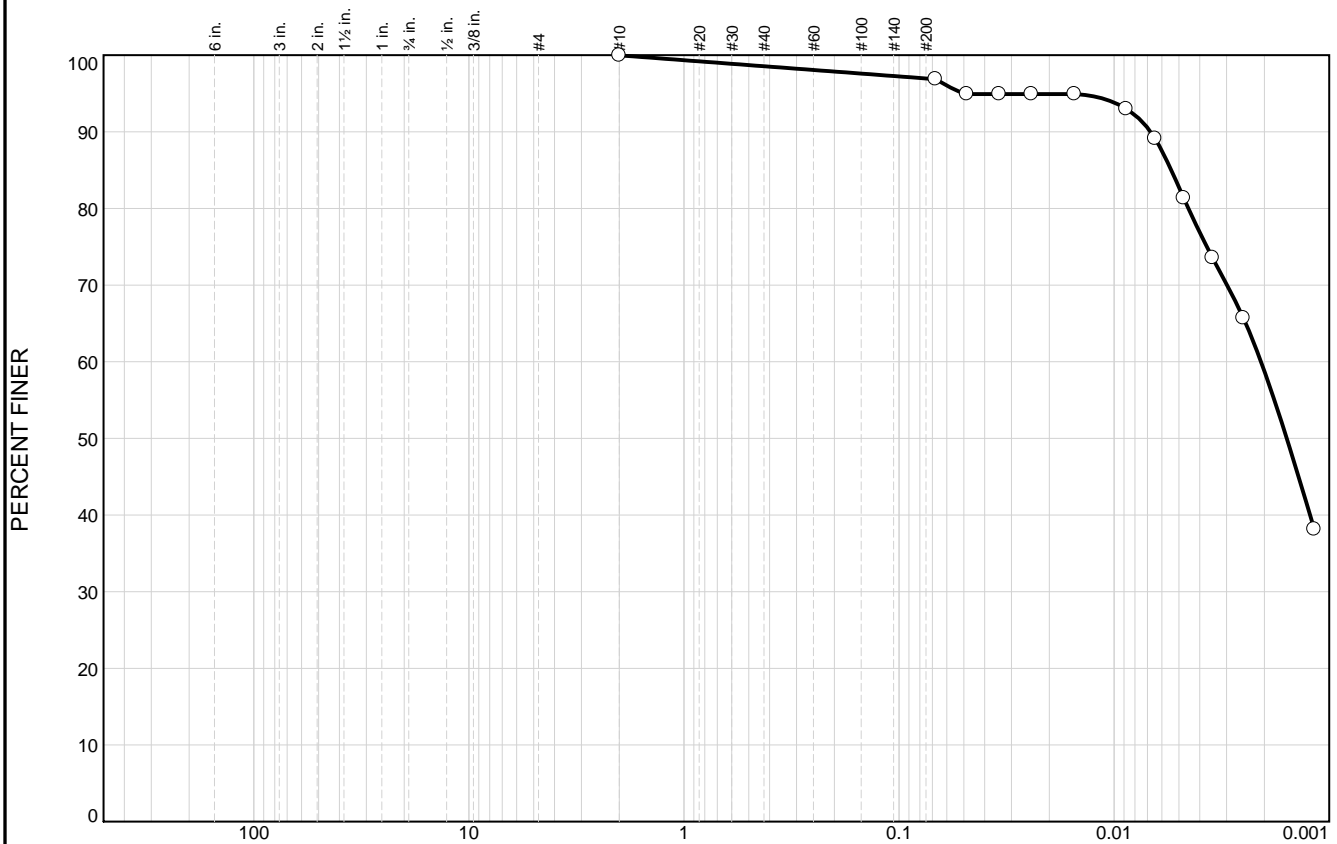
Particle Size Distribution Report



GRAIN SIZE - mm.										
% +3"		% Gravel		% Sand			% Fines			
		Coarse	Fine	Coarse	Medium	Fine	Silt		Clay	
○	0.0	22.8	12.4	7.6	9.8	8.2	39.2			
×	LL	PL	D ₈₅	D ₆₀	D ₅₀	D ₃₀	D ₁₅	D ₁₀	C _c	C _u
○			27.6551	3.2122	0.6383					
Material Description								USCS	AASHTO	
○ DARK BROWN TO BLACK SILTY C/F GRAVEL, SM M/F/C SAND								GM		
Project No. 195651 Client: TRANSMISSION DEVELOPERS INC. Project: TDI CHAMPLAIN HUDSON POWER EXPRESS - CSX ○ Sample Source: B219.5-1 Depth: 6.0-10.0 FT Sample No.: S-4 & S-5								Remarks: ○SAMPLE DESCRIPTION BASED ON VISUAL IDENTIFICAITON AND LABORATORY ANALYSIS		
TRC Engineers, Inc. Mt. Laurel, NJ										
								Figure 111		

Tested By: TBT 01/10/13 Checked By: JPB 03/12/13

Particle Size Distribution Report



GRAIN SIZE - mm.

	% +3"		% Gravel		% Sand			% Fines		
			Coarse	Fine	Coarse	Medium	Fine	Silt	Clay	
<input type="radio"/>						1.4	1.6	14.2	82.8	
<input type="checkbox"/>	LL	PL	D ₈₅	D ₆₀	D ₅₀	D ₃₀	D ₁₅	D ₁₀	C _c	C _u
<input type="radio"/>			0.0054	0.0021	0.0016					

Material Description

USCS

AASHTO

☐ LIGHT BROWN TO BROWN CLAY, TR TO SM SILT, TR F/M SAND

Project No. 195651 Client: TRANSMISSION DEVELOPERS INC.

Project: TDI CHAMPLAIN HUDSON POWER EXPRESS - CSX

☐ Source of Sample: B219.5-1 Depth: 13.5-15.0 FT Sample Number: S-6

TRC Engineers, Inc.

Mt. Laurel, NJ

Remarks:

☐ SAMPLE DESCRIPTION
BASED ON VISUAL
IDENTIFICATION AND
LABORATORY ANALYSIS

Figure 112

Tested By: TBT 01/08/13 Checked By: JPB 03/12/13

EXPLORATION PLAN

Champlain-Hudson Power Express- Phase 4 HDD Borings – Package 6 and 7
Schenectady through Selkirk, NY
April 25, 2023 ■ Terracon Project No. JB215256J



Geotechnical Data Report

Champlain-Hudson Power Express- Phase 4 HDD Borings – Package 6 and 7A – Rev 1
Schenectady through Selkirk, NY
April 25, 2023 ■ Terracon Project No. JB215256J



Rock Core – Boring KB-207.1 Run 13 through Run 15



Rock Core – Boring KB-219.4 Run 1 through Run 4

Geotechnical Data Report

Champlain-Hudson Power Express- Phase 4 HDD Borings – Package 6 and 7A – Rev 1

Schenectady through Selkirk, NY

April 25, 2023 ■ Terracon Project No. JB215256J



Rock Core – Boring KB-219.4 Run 5 through Run 8



Rock Core – Boring KB-219.4 Run 9 through Run 12











BORING LOG NO. KB-219.4

Page 1 of 4

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES			
	Latitude: 42.2497° Longitude: -73.8558°								LL-PL-PI				
	DEPTH	ELEVATION (Ft.)											
	0.3	120.4	5			10	1-2-3-3 N=5			32			
		4.0				116.7	20				5-6-8-8 N=14	11.8	
						20	6-5-8-8 N=13				18-16-8-7 N=24		
						22	10-10-14-38 N=24	50/0"					
						12	25-17-20-15 N=37						REC=100% RQD=85%
						12							
15.0	105.7	15											
	20.0	100.7	20										
	25.0	95.7	25										

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-15' 4" Casing
15-20' Mud Rotary
20' -75' NQ Core Barrel

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (if any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 89.1% +/-4.4%
Hammer Efficiency Correction (CE): 1.49
Logged by JCH/DO

WATER LEVEL OBSERVATIONS

No free water encountered

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 02-15-2023

Drill Rig: Mobil B-57

Project No.: JB215256J

Boring Completed: 02-16-2023

Driller: J. Swope

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE GDT 4/21/23

Page 2 of 4

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

GRAPHIC LOG	LOCATION	See Exploration Plan	DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2497° Longitude: -73.8558°								LL-PL-PI	
	DEPTH	Surface Elev.: 120.73 (Ft.)	ELEVATION (Ft.)							
		SHALE , occasional calcite veins, inter bedded with greywacke, unweathered, very close to wide fractured, good RQD, gray					REC=95% RQD=78%			
	30.0		90.7	30						
		SHALE , occasional calcite veins, unweathered, close to wide fractured, excellent RQD, gray					REC=100% RQD=90%			
	35.0		85.7	35						
		GREYWACKE , occasional calcite veins, inter bedded with shale, unweathered, very close to wide fractured with occasional high angled fractures, excellent RQD, gray					REC=100% RQD=96%			
	40.0		80.7	40						
		SHALE , occasional calcite veins, inter bedded with greywacke, unweathered, close to moderate fractured, good RQD, gray					REC=100% RQD=80%			
	45.0		75.7	45						
		SHALE , occasional calcite veins, inter bedded with greywacke, unweathered, close to moderate fractured, fair RQD, gray					REC=100% RQD=53%			
	50.0		70.7	50						

Hammer Type: Automatic

Project No.: JB215256J

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS.GPJ TERRACON DATATEMPLATE.GDT 4/21/23

Page 3 of 4

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

GRAPHIC LOG	LOCATION	See Exploration Plan	DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2497° Longitude: -73.8558°								LL-PL-PI	
	DEPTH	Surface Elev.: 120.73 (Ft.) ELEVATION (Ft.)								
		GREYWACKE , occasional calcite veins, inter bedded with shale, unweathered, very close to close fractured with occasional high angled fractures, good RQD, gray					REC=100% RQD=78%			
	55.0	65.7	55							
		SHALE , occasional calcite veins, inter bedded with greywacke, unweathered, close to moderate fractured with occasional high angled fractures, excellent RQD, gray					REC=100% RQD=95%			
	60.0	60.7	60							
		GREYWACKE , occasional calcite veins, inter bedded with shale, unweathered, wide fractured with occasional high angled fractures, excellent RQD, gray					REC=100% RQD=100%			
	65.0	55.7	65							
		GREYWACKE , occasional calcite veins, unweathered, extremely close to wide fractured with occasional high angled fractures, good RQD, gray					REC=96% RQD=78%			
	70.0	50.7	70							
		SHALE , occasional calcite veins, unweathered, extremely close to moderate fractured with occasional high angled fractures, good RQD, gray					REC=100% RQD=70%			
	75.0	45.7	75							

Hammer Type: Automatic

Project No.: JB215256J

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT, GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS.GPJ TERRACON DATATEMPLATE.GDT 4/21/23



BORING LOG NO. KB-219.4

Page 4 of 4

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan	DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2497° Longitude: -73.8558°							LL-PL-PI	
	DEPTH	ELEVATION (Ft.)							
	SHALE , occasional calcite veins, inter bedded with greywacke, unweathered, very close to close fractured with occasional high angled fractures, fair RQD, gray					REC=100% RQD=60%			
	Boring Terminated at 80 Feet	80							
Stratification lines are approximate. In-situ, the transition may be gradual.									
Hammer Type: Automatic									
Advancement Method: 00-15' 4" Casing 15-20' Mud Rotary 20' -75' NQ Core Barrel			See Exploration and Testing Procedures for a description of field and laboratory procedures used and additional data (If any). See Supporting Information for explanation of symbols and abbreviations. Elevations were provided by others.			Notes: Hammer Efficiency Summary: Energy Transfer Ratio: 89.1% +/-4.4% Hammer Efficiency Correction (CE): 1.49 Logged by JCH/DO			
Abandonment Method: Boring backfilled with bentonite grout upon completion									
WATER LEVEL OBSERVATIONS			 30 Corporate Cir Ste 201 Albany, NY			Boring Started: 02-15-2023		Boring Completed: 02-16-2023	
No free water encountered						Drill Rig: Mobil B-57		Driller: J. Swope	
						Project No.: JB215256J			

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS.GPJ TERRACON_DATATEMPLATE.GDT 4/21/23

Sheet 1 of 1

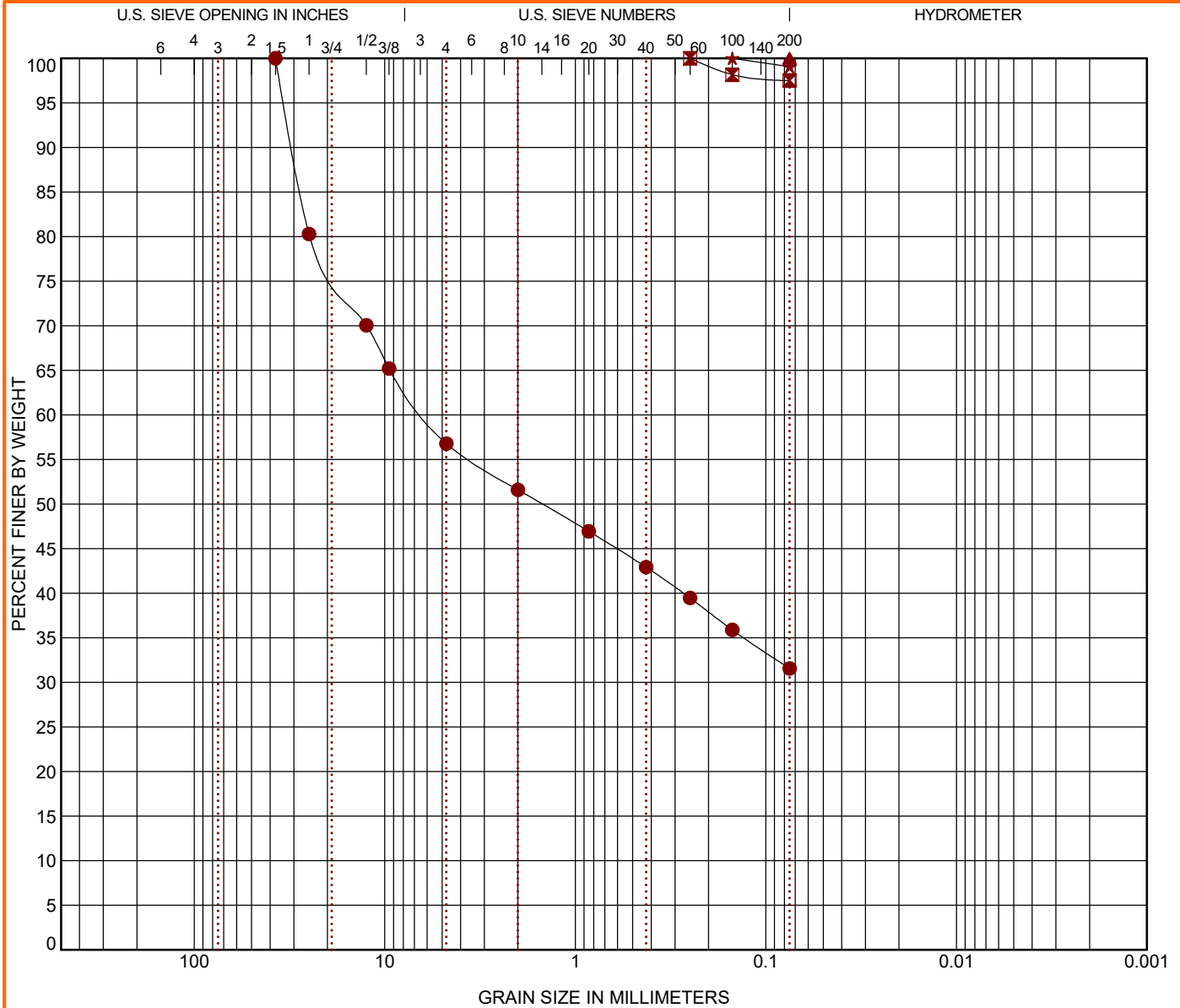
BORING ID	Depth (Ft.)	Water Content (%)	Liquid Limit	Plastic Limit	Plasticity Index	Organic Content (%)
KB-206.8	4-6	29.4	50	26	24	
KB-206.8	15-17	32.9	40	23	17	
KB-206.8	35-37	11.0	17	13	4	
KB-207.0	4-6	23.7	42	30	12	
KB-207.1	4-6	15.1				
KB-209.7	4-6	30.3	64	32	32	2.8
KB-209.7	15-17	38.8	64	32	32	
KB-209.7	25-27	38.8	54	25	29	
KB-209.7	40-42	38.8	45	25	20	
KB-211.4B	4-6	32.8	58	32	26	
KB-211.4B	15-17	48.0	55	31	24	
KB-211.4B	40-42	36.7	63	32	31	
KB-214.4	4-6	33.7	65	33	32	
KB-214.4	15-17	37.6	57	29	28	
KB-214.4	30-32	49.7	45	30	15	
KB-219.4	6-8	11.8				
KB-220.9	4-6	31.0	50	27	23	
KB-220.9	20-22	39.6	47	26	21	
KB-220.9	45-47	33.6	42	27	15	

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

LABORATORY TESTS ARE NOT VALID IF SEPARATED FROM ORIGINAL REPORT. SMART LAB SUMMARY-PORTRAIT JB215256J PHASE 4 BORINGS.GPJ TERRACON_DATA\TEMPLATE.GDT 4/14/23

GRAIN SIZE DISTRIBUTION

ASTM D422 / ASTM C136



Client

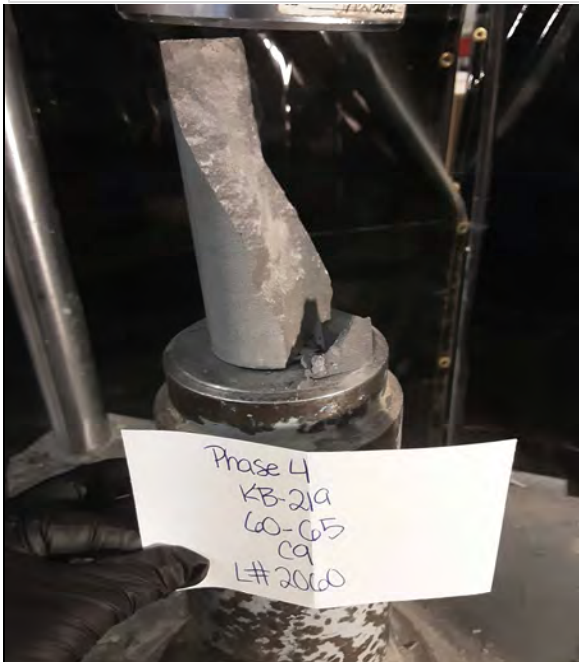
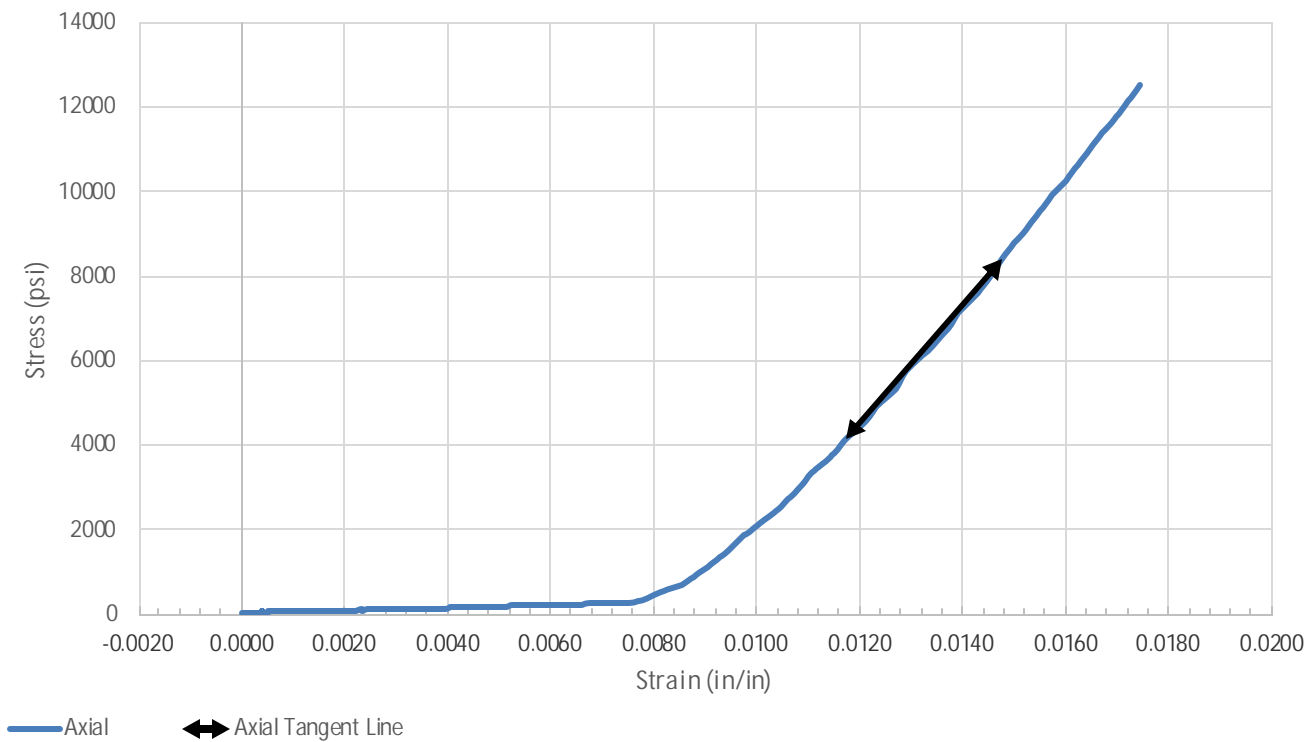
Kiewit Engineering

Project

Phase 4 Borings

Project No. JB215256J

ASTM D7012 Stress/ Strain Curve



Phase 4
KB-219
60-65
C9
L# 2060

SAMPLE LOCATION			
Site:	Phase 4 Borings		
Description:	Greywacke		
Boring:	KB-219.4	Depth (feet):	60.0-65.0
SPECIMEN INFORMATION			
Sample No.:	C-9	Mass (g):	564.96
Length (in.):	4.12	Diameter (in.):	1.98
L/D Ratio:	2.08	Density (pcf):	169.66
TEST RESULTS			
Failure Load (lbs):		38578	
Failure Strain (in/in):		0.020	
Unconfined Compressive Strength (psi):		12,529	
Elastic Modulus, E, (ksi):		1403	
Time of Failure (min):		03:20	
Rate of Loading (in/sec):		0.04	
Moisture Content Post-break:		0.40%	

Rock Core D7012 Method C



Client	Project
Kiewit Engineering	Phase 4 Borings

Project No. JB215256J

Equipment:	TICCS ID:
Calipers	W-44049
Scale	B-71466
Dial Indicator	C-70608
Compression (spherically seated)	C-48999

Samples were prepared and tested in accordance with ASTM D4543 and D7012. Deviations, if any, are noted below:

Notes:

Per ASTM D4543, this specimen has not met the requirements for flatness, by exceeding 0.001 inches.

Per ASTM D4543, this specimen has not met the requirements for parallelism, by exceeding 0.25°.

Per ASTM D4543, this specimen has not met the requirements for flatness, by exceeding 0.001 inches.

Per ASTM D4543 and ASTM D7012, the desired specimen length to diameter are between 2.0:1 and 2.5:1.

According to ASTM D7012 Section 8.2.1, this specimen, although not meeting all requirements of ASTM D4543 is acceptable for testing. However, the results reported may differ from results obtained from a test specimen that meets the requirements of D4543.

Client

Kiewit Engineering

Project

Phase 4 Borings

Project No. JB215256J

Splitting Tensile Strength of Intact Rock Core Specimens, ASTM D3967

Boring	KB-219.4	Material Description			Greywacke	
Sample No	C-9	Equipment Used			Tinius Olsen (120,000lbs)	
Depth (ft)	60.0-65.0	TICCS ID/Serial No.			C-48999, 118285	
Lab No	2060	Calibration Date			11/2/2022	
		TENSILE STRENGTH				
Lab No.	1	2	3	4	5	
Diameter (in)	1.98	1.98	1.98	1.98	--	
Length (in)	0.64	0.68	0.68	0.70	--	
Length Diameter Ratio	0.32	0.34	0.34	0.35	--	
Rate of Loading	0.0064	0.0068	0.0068	0.0070	--	
Moisture Condition	0.43%	0.43%	0.43%	0.43%	--	
Maximum Applied Load (lbf)	4851	6229	4557	4142	--	
Splitting Tensile Strength (psi)	2438.3	2946.8	2155.8	1903.5	--	
		TENSILE STRENGTH				
Lab No.	6	7	8	9	10	
Diameter (in)	--	--	--	--	--	
Length (in)	--	--	--	--	--	
Length Diameter Ratio	--	--	--	--	--	
Rate of Loading	--	--	--	--	--	
Moisture Condition	--	--	--	--	--	
Maximum Applied Load (lbf)	--	--	--	--	--	
Splitting Tensile Strength (psi)	--	--	--	--	--	

Client: Terracon Consultants, Inc.		
Project: Champlain-Hudson Power Express		
Location: ---	Project No: GTX-316884	
Boring ID: KB-219.4	Sample Type: cylinder	Tested By: tlm
Sample ID: ---	Test Date: 03/09/23	Checked By: smd
Depth : 60'-65'	Test Id: 707603	
Test Comment: ---		
Visual Description: ---		
Sample Comment: ---		

Abrasiveness of Rock Using the Cerchar Method by ASTM D7625

Boring ID	Sample ID	Depth	Stylus No	Reading 1	Reading 2	Average	Comments
KB-219.4	---	60-65 ft	1	0.2	0.2	0.20	
			2	0.3	0.4	0.35	
			3	0.3	0.4	0.35	
			4	0.2	0.2	0.20	
			5	0.3	0.4	0.35	
			Average CAIs			0.29	
			Average CAI *			0.77	
CERCHAR Abrasiveness Index Classification					Low abrasiveness		

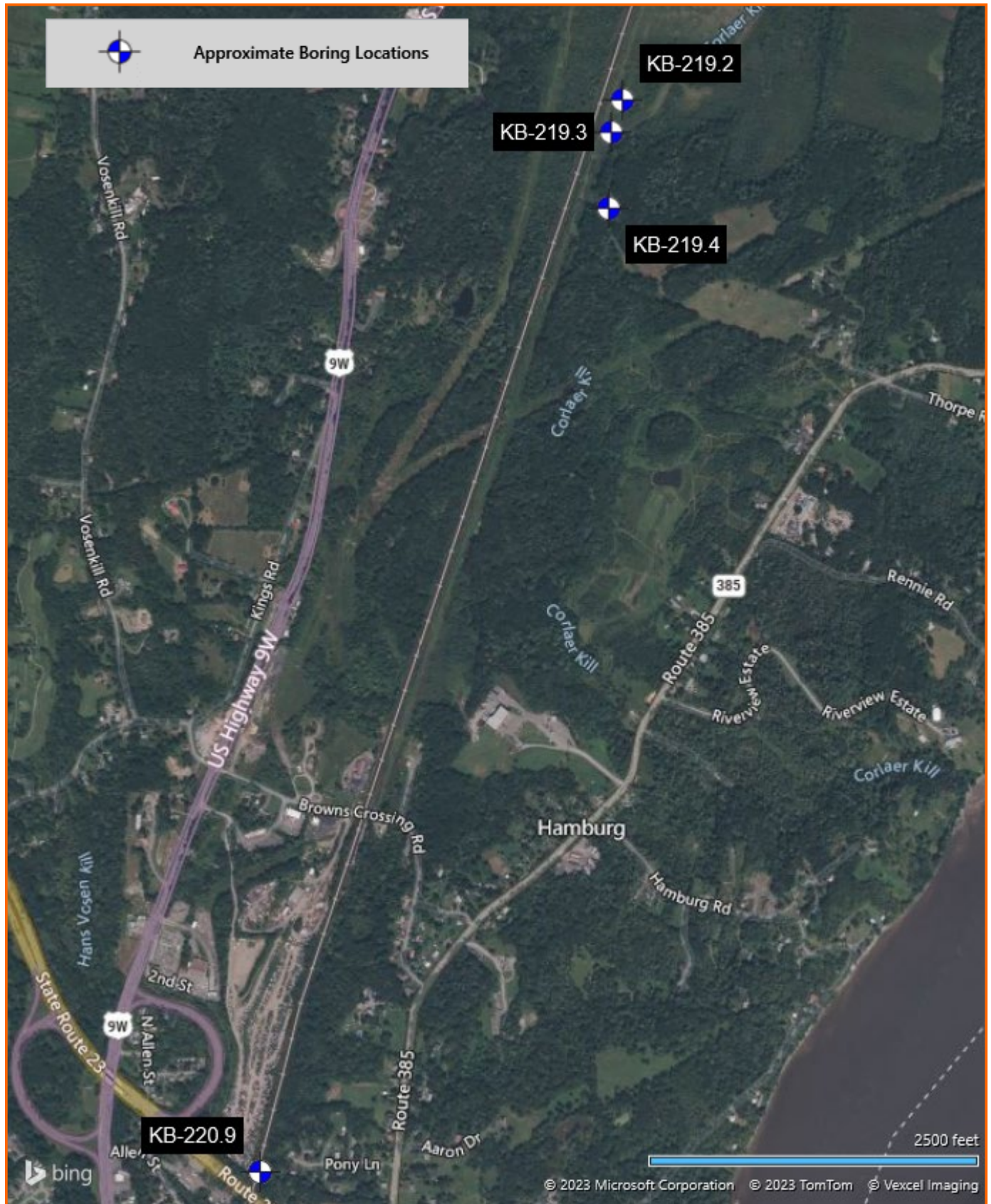
Notes

Test Surface: Saw Cut
 Moisture Condition: As Received
 Apparatus Type: Original CERCHAR
 Stylus Hardness: Rockwell Hardness 40/42 HRC
 Stylus Displacement Relative to Rock Fabric:
 Styli 1-3: Normal; Styli 4-5: Parallel
 * CAI = (0.99 * CAIs) + 0.48
 CAIs = CERCHAR index for smooth (saw cut) surface
 CAI = CERCHAR index for natural surface
 Comments:



EXPLORATION PLAN

Champlain-Hudson Power Express- Phase 4 HDD Borings – Package 6 and 7
Schenectady through Selkirk, NY
May 31, 2023 ■ Terracon Project No. JB215256J





BORING LOG NO. KB-219.2

Page 1 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2519° Longitude: -73.8554°								LL-PL-PI	
	DEPTH	ELEVATION (Ft.)								
	0.4	116.3								
	TOPSOIL									
	LEAN CLAY (CL) , varved silt and clay, brown, very soft to very stiff									
						12	1-1-2-3 N=3			
						18	3-4-6-9 N=10			
	5					10	4-4-9-10 N=13	27.5	42-23-19	96
						24	11-12-13-14 N=25			
						24	11-9-8-8 N=17			
	10					24	WH/18"-4			
										
	15					24	WH/12"-3-4 N=3			

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-57" Mud Rotary

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (if any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer
WR = Weight of rod

WATER LEVEL OBSERVATIONS

No free water encountered

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-20-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-21-2023

Driller: S. Morey

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE GDT 5/31/23










BORING LOG NO. KB-219.2

Page 2 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2519° Longitude: -73.8554°								LL-PL-PI	
DEPTH		Surface Elev.: 116.683 (Ft.)	ELEVATION (Ft.)							
	<u>ELASTIC SILT (MH)</u> , varved silt and clay, gray, very soft <i>(continued)</i>					24	WH/24"			
	30									
	35									
40.0	<u>LEAN CLAY (CL)</u> , varved silt and clay, gray, very soft to soft		76.7	40		24	WR/24"	43.4	41-24-17	94
										
	45									

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-57" Mud Rotary

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (If any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer
WR = Weight of rod

WATER LEVEL OBSERVATIONS

No free water encountered

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-20-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-21-2023

Driller: S. Morey

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS GPJ TERRACON_DATATEMPLATE.GDT 5/31/23


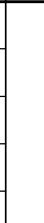



BORING LOG NO. KB-219.2

Page 3 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2519° Longitude: -73.8554°								LL-PL-PI	
DEPTH ELEVATION (Ft.)										
	<u>LEAN CLAY (CL)</u> , varved silt and clay, gray, very soft to soft <i>(continued)</i>		55			8	WH/12"-4-4 N=4			
	55.0	61.7								
	<u>SANDY SILT WITH GRAVEL (SM)</u> , gray, hard, (GLACIAL TILL)					10	12-23-15-50/3" N=38			
	56.8	59.9								
Boring Terminated at 56.75 Feet										

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-57" Mud Rotary

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (If any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer
WR = Weight of rod

WATER LEVEL OBSERVATIONS

No free water encountered

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-20-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-21-2023

Driller: S. Morey

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS.GPJ TERRACON_DATATEMPLATE.GDT 5/31/23



BORING LOG NO. KB-219.3

Page 1 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2512° Longitude: -73.8557°								LL-PL-PI	
	DEPTH	ELEVATION (Ft.)								
	0.4	114.8								
	TOPSOIL									
	FAT CLAY (CH) , varved silt and clay, brown, soft to very stiff					12	1-2-2-2 N=4			
						14	2-4-7-8 N=11			
			5			16	6-8-10-11 N=18	29.3	55-29-26	98
						20	11-11-12-11 N=23			
						22	11-10-10-12 N=20			
			10			24	3-4-6-4 N=10			
			15			24	2-3-4-4 N=7	39.5	51-26-25	96
	20.0	95.2	20			24	WH/24"			
	LEAN CLAY (CL) , varved silt and clay, gray, very soft									
			25							

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-52" 3" Casing

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (If any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer

WATER LEVEL OBSERVATIONS

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-19-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-20-2023

Driller: S. Morey

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE GDT 5/31/23

BORING LOG NO. KB-219.3

Page 2 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan		DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
	Latitude: 42.2512° Longitude: -73.8557°								LL-PL-PI	
DEPTH		ELEVATION (Ft.)								
	<u>LEAN CLAY (CL)</u> , varved silt and clay, gray, very soft (<i>continued</i>)		30		X	24	WH/24"			
	35.0	80.2	35		X	24	WH/24"	23.5	27-18-9	73
			40		X	1	6-6-6-3 N=12			
	42.0	73.2	45		X	18	15-7-3-50 N=10	15.6		65
	<u>SANDY SILT (ML)</u> , gray, stiff to hard, (GLACIAL TILL)									
			50							

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-52' 3" Casing

Abandonment Method:
Boring backfilled with bentonite grout upon completion

See [Exploration and Testing Procedures](#) for a description of field and laboratory procedures used and additional data (if any).

See [Supporting Information](#) for explanation of symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer

WATER LEVEL OBSERVATIONS

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-19-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-20-2023

Driller: S. Morey

THIS BORING LOG IS NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GEO SMART LOG-NO WELL JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE GDT 5/31/23


BORING LOG NO. KB-219.3

Page 3 of 3

PROJECT: Phase 4 Borings

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

SITE: Champlain to Hudson HDD Crossings

GRAPHIC LOG	LOCATION See Exploration Plan Latitude: 42.2512° Longitude: -73.8557° Surface Elev.: 115.191 (Ft.)	DEPTH (Ft.)	WATER LEVEL OBSERVATIONS	SAMPLE TYPE	RECOVERY (In.)	FIELD TEST RESULTS	WATER CONTENT (%)	ATTERBERG LIMITS	PERCENT FINES
								LL-PL-PI	
DEPTH	ELEVATION (Ft.)								
	SANDY SILT (ML) , gray, stiff to hard, (GLACIAL TILL) (<i>continued</i>)				10	16-15-17-18 N=32			
52.0	63.2								
Boring Terminated at 52 Feet									

Stratification lines are approximate. In-situ, the transition may be gradual.

Hammer Type: Automatic

Advancement Method:
0-10 4" Casing
10'-52' 3" CasingAbandonment Method:
Boring backfilled with bentonite grout upon completionSee [Exploration and Testing Procedures](#) for a
description of field and laboratory procedures
used and additional data (if any).See [Supporting Information](#) for explanation of
symbols and abbreviations.

Elevations were provided by others.

Notes:

Hammer Efficiency Summary:
Energy Transfer Ratio: 84.7% +/-5.0%
Hammer Efficiency Correction (CE): 1.41
Logged by DOL
WH = Weight of hammer

WATER LEVEL OBSERVATIONS

Terracon
30 Corporate Cir Ste 201
Albany, NY

Boring Started: 04-19-2023

Drill Rig: Diedrich D-50

Project No.: JB215256J

Boring Completed: 04-20-2023

Driller: S. Morey

Summary of Laboratory Results

Sheet 1 of 1

BORING ID	Depth (Ft.)	Water Content (%)	Liquid Limit	Plastic Limit	Plasticity Index
KB-206.8	4-6	29.4	50	26	24
KB-206.8	15-17	32.9	40	23	17
KB-206.8	35-37	11.0	17	13	4
KB-207.0	4-6	23.7	42	30	12
KB-207.1	4-6	15.1			
KB-211.4B	4-6	32.8	58	32	26
KB-211.4B	15-17	48.0	55	31	24
KB-211.4B	40-42	36.7	63	32	31
KB-214.4	4-6	33.7	65	33	32
KB-214.4	15-17	37.6	57	29	28
KB-214.4	30-32	49.7	45	30	15
KB-219.2	4-6	27.5	42	23	19
KB-219.2	20-22	40.8	50	35	15
KB-219.2	40-42	43.4	41	24	17
KB-219.3	4-6	29.3	55	29	26
KB-219.3	15-17	39.5	51	26	25
KB-219.3	35-37	23.5	27	18	9
KB-219.3	45-47	15.6			
KB-220.9	4-6	31.0	50	27	23
KB-220.9	20-22	39.6	47	26	21
KB-220.9	45-47	33.6	42	27	15

PROJECT: Phase 4 Borings

SITE: Champlain to Hudson HDD Crossings

Terracon
30 Corporate Cir Ste 201
Albany, NY

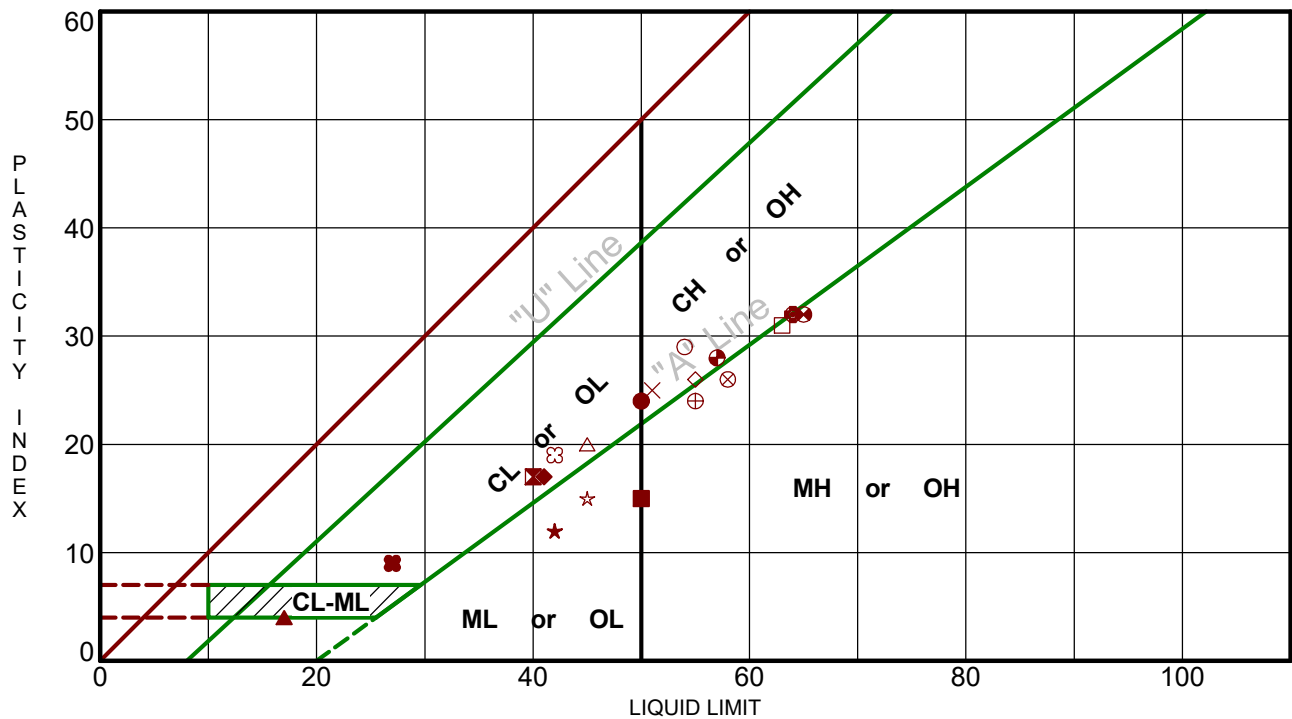
PROJECT NUMBER: JB215256J

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

LABORATORY TESTS ARE NOT VALID IF SEPARATED FROM ORIGINAL REPORT. SMART LAB SUMMARY-PORTRAIT JB215256J PHASE 4 BORINGS.GPJ TERRACON_DATA\TEMPLATE.GDT 5/30/23

ATTERBERG LIMITS RESULTS

ASTM D4318



Boring ID	Depth (Ft)	LL	PL	PI	Fines	USCS	Description
● KB-206.8	4 - 6	50	26	24	87.8	CH	FAT CLAY
⊠ KB-206.8	15 - 17	40	23	17	99.4	CL	LEAN CLAY
▲ KB-206.8	35 - 37	17	13	4	37.5	SC-SM	SILTY, CLAYEY SAND with GRAVEL
★ KB-207.0	4 - 6	42	30	12	86.9	ML	SILT
⊙ KB-209.7	4 - 6	64	32	32	100.0	MH	ELASTIC SILT
⊕ KB-209.7	15 - 17	64	32	32	100.0	MH	ELASTIC SILT
○ KB-209.7	25 - 27	54	25	29	100.0	CH	FAT CLAY
△ KB-209.7	40 - 42	45	25	20	100.0	CL	LEAN CLAY
⊗ KB-211.4B	4 - 6	58	32	26	53.8	MH	SANDY ELASTIC SILT
⊕ KB-211.4B	15 - 17	55	31	24	82.0	MH	ELASTIC SILT with SAND
□ KB-211.4B	40 - 42	63	32	31	96.7	MH	ELASTIC SILT
⊗ KB-214.4	4 - 6	65	33	32	84.2	MH	ELASTIC SILT with SAND
⊕ KB-214.4	15 - 17	57	29	28	94.7	CH	FAT CLAY
★ KB-214.4	30 - 32	45	30	15	93.2	ML	SILT
⊗ KB-219.2	4 - 6	42	23	19	96.5	CL	LEAN CLAY
■ KB-219.2	20 - 22	50	35	15	99.4	MH	ELASTIC SILT
◆ KB-219.2	40 - 42	41	24	17	93.9	CL	LEAN CLAY
◇ KB-219.3	4 - 6	55	29	26	98.3	CH	FAT CLAY
× KB-219.3	15 - 17	51	26	25	95.6	CH	FAT CLAY
⊕ KB-219.3	35 - 37	27	18	9	73.3	CL	LEAN CLAY with SAND

PROJECT: Phase 4 Borings

SITE: Champlain to Hudson HDD Crossings

Terracon
30 Corporate Cir Ste 201
Albany, NY

PROJECT NUMBER: JB215256J

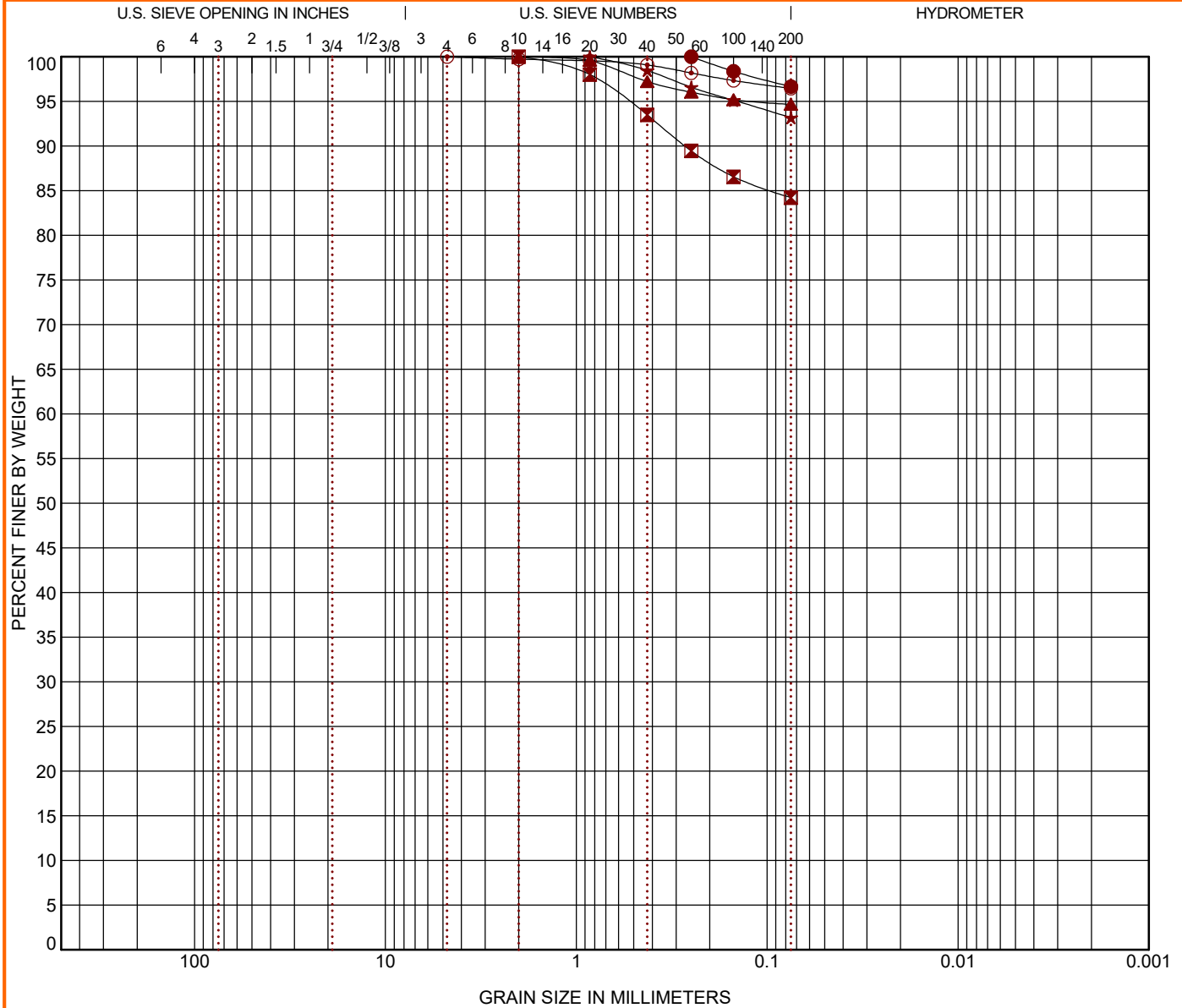
CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

LABORATORY TESTS ARE NOT VALID IF SEPARATED FROM ORIGINAL REPORT. ATTERBERG LIMITS JB215256J PHASE 4 BORINGS.GPJ TERRACON_DATATEMPLATE.GDT 5/31/23

GRAIN SIZE DISTRIBUTION

ASTM D422 / ASTM C136

LABORATORY TESTS ARE NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GRAIN SIZE: USCS-2 JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE.GDT 5/31/23



COBBLES	GRAVEL		SAND			SILT OR CLAY
	coarse	fine	coarse	medium	fine	

Boring ID	Depth (Ft)	USCS Classification				WC (%)	LL	PL	PI	Cc	Cu
● KB-211.4B	40 - 42	ELASTIC SILT (MH)				36.7	63	32	31		
☒ KB-214.4	4 - 6	ELASTIC SILT with SAND (MH)				33.7	65	33	32		
▲ KB-214.4	15 - 17	FAT CLAY (CH)				37.6	57	29	28		
★ KB-214.4	30 - 32	SILT (ML)				49.7	45	30	15		
⊙ KB-219.2	4 - 6	LEAN CLAY (CL)				27.5	42	23	19		
Boring ID	Depth (Ft)	D ₁₀₀	D ₆₀	D ₃₀	D ₁₀	%Cobbles	%Gravel	%Sand	%Silt	%Fines	%Clay
● KB-211.4B	40 - 42	0.25				0.0	0.0	3.3		96.7	
☒ KB-214.4	4 - 6	2				0.0	0.0	15.8		84.2	
▲ KB-214.4	15 - 17	2				0.0	0.0	5.3		94.7	
★ KB-214.4	30 - 32	0.85				0.0	0.0	6.8		93.2	
⊙ KB-219.2	4 - 6	4.75				0.0	0.0	3.5		96.5	

PROJECT: Phase 4 Borings

SITE: Champlain to Hudson HDD Crossings

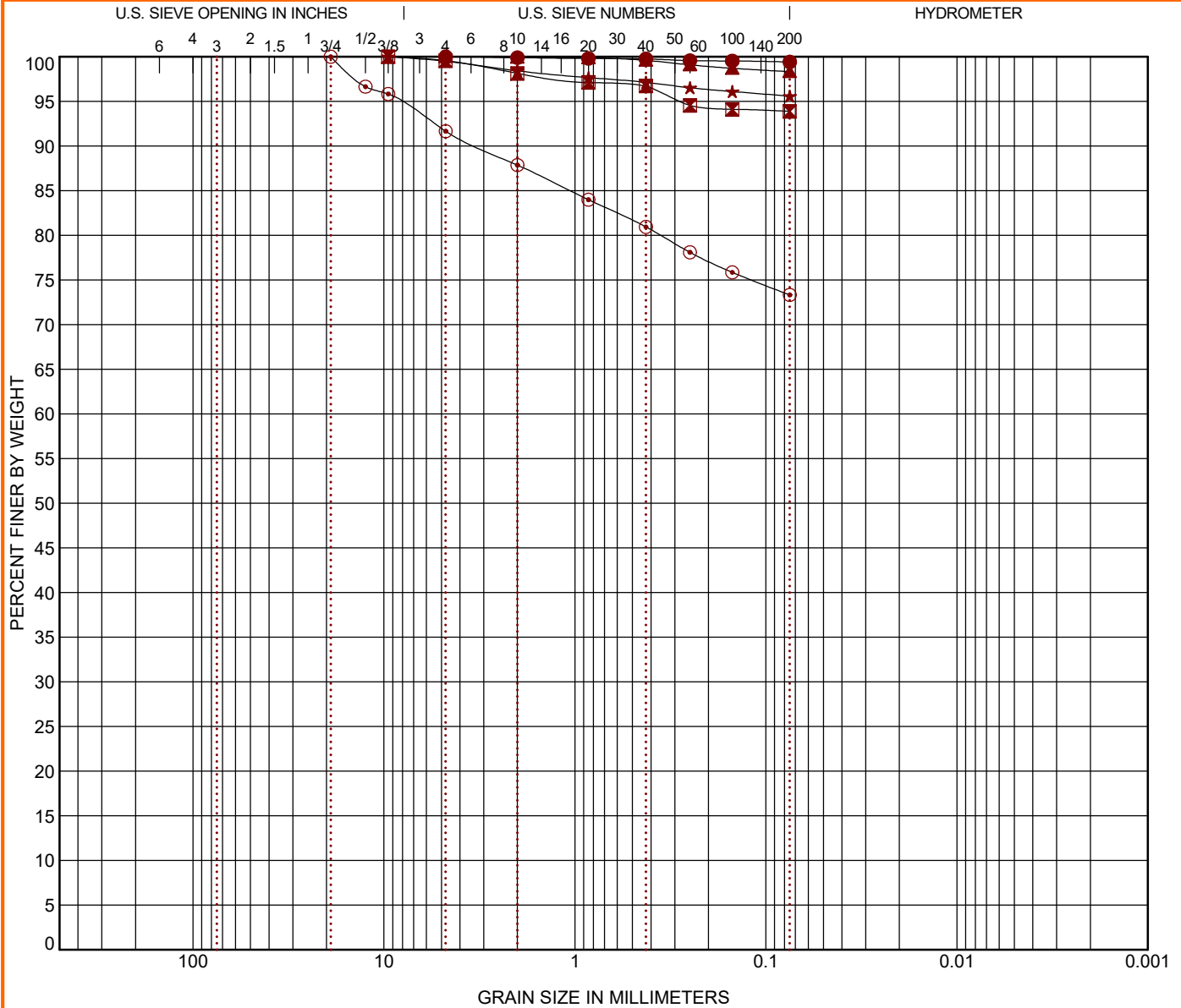
Terracon
30 Corporate Cir Ste 201
Albany, NY

PROJECT NUMBER: JB215256J

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

GRAIN SIZE DISTRIBUTION

ASTM D422 / ASTM C136



COBBLES	GRAVEL		SAND			SILT OR CLAY
	coarse	fine	coarse	medium	fine	

Boring ID	Depth (Ft)	USCS Classification				WC (%)	LL	PL	PI	Cc	Cu
● KB-219.2	20 - 22	ELASTIC SILT (MH)				40.8	50	35	15		
☒ KB-219.2	40 - 42	LEAN CLAY (CL)				43.4	41	24	17		
▲ KB-219.3	4 - 6	FAT CLAY (CH)				29.3	55	29	26		
★ KB-219.3	15 - 17	FAT CLAY (CH)				39.5	51	26	25		
⊙ KB-219.3	35 - 37	LEAN CLAY with SAND (CL)				23.5	27	18	9		
Boring ID	Depth (Ft)	D ₁₀₀	D ₆₀	D ₃₀	D ₁₀	%Cobbles	%Gravel	%Sand	%Silt	%Fines	%Clay
● KB-219.2	20 - 22	4.75				0.0	0.0	0.6		99.4	
☒ KB-219.2	40 - 42	9.5				0.0	0.4	5.7		93.9	
▲ KB-219.3	4 - 6	4.75				0.0	0.0	1.7		98.3	
★ KB-219.3	15 - 17	9.5				0.0	0.5	3.9		95.6	
⊙ KB-219.3	35 - 37	19				0.0	8.3	18.3		73.3	

PROJECT: Phase 4 Borings

SITE: Champlain to Hudson HDD Crossings

Terracon
30 Corporate Cir Ste 201
Albany, NY

PROJECT NUMBER: JB215256J

CLIENT: Kiewit Engineering (NY) Corp
Lone Tree, CO

LABORATORY TESTS ARE NOT VALID IF SEPARATED FROM ORIGINAL REPORT. GRAIN SIZE: USCS-2 JB215256J PHASE 4 BORINGS GPJ TERRACON DATATEMPLATE.GDT 5/31/23

Appendix C

Calculation Package

Defining Parameters of Horizontal Directional Drilling :

$$D_1 := 10.75 \text{ in}$$

Pipe 1 outer diameter

$$D_2 := 2.375 \text{ in}$$

Pipe 2 outer diameter

$$D_{rod} := 3.5 \text{ in}$$

Assumed drill rod diameter

$$DR_1 := 9$$

Dimension ratio of Pipe 1

$$DR_2 := 11$$

Dimension ratio of Pipe 2

$$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$$

Thickness of Pipe 1

$$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$$

Thickness of Pipe 2

$$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$$

Pipe circumference of pipe 1

$$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$$

Pipe circumference of pipe 2

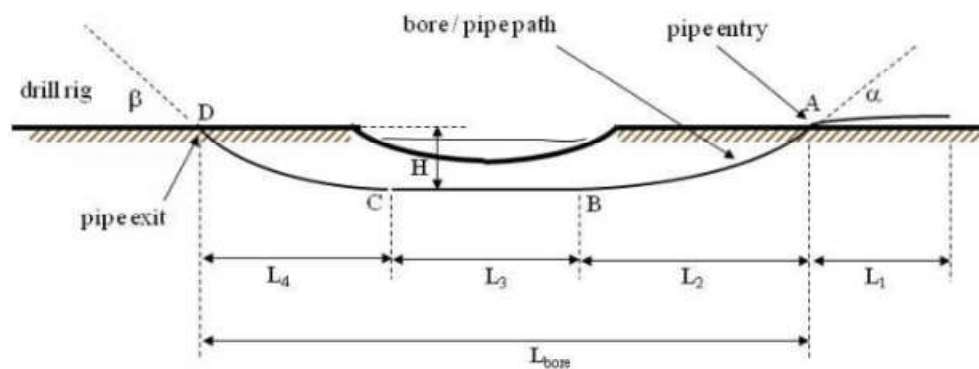


Illustration 1 - Schematic of Drive Cross-section

$$\alpha := 8^\circ$$

$$\alpha_{in} := \alpha = 0.1396 \text{ rad}$$

Borehole entry angle (degrees, radians)

$$\beta := 8^\circ$$

$$\beta_{exit} := \beta = 0.1396 \text{ rad}$$

Borehole exit angle (degrees, radians)

$$D_r := 18 \cdot \text{in}$$

Final reamed bore diameter

$$H_{max} := 40.0 \text{ ft}$$

Max depth of bore hole to final reamed bore diameter

$$H_{max1} := H_{max} + \frac{D_r}{2} = 40.75 \text{ ft}$$

Max depth to bore hole springline from ground surface

$$L_{total} := 551.2 \text{ ft}$$

Total length of HDD crossing

$$L_1 := 150 \text{ ft}$$

Assumed pipe drag on surface, See Illustration 1

$$L_2 := 203.7 \text{ ft}$$

Horizontal length to achieve depth - provided by Contractor, See Illustration 1

$$L_3 := 149.1 \text{ ft}$$

Straight horizontal section

$$L_4 := 198.4 \text{ ft}$$

Horizontal distance to rise to surface, See Illustration 1

$$H := 18.0 \text{ ft}$$

Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 90 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.4$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 51.2 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 589 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 6192 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 8352 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 11711 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 12508 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 24.6 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 589 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} (T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 3392 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 4363 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 5904 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 5904 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 12022 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 485 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 5674 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 229 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

check := if ($P_{SPF1} > P_{11}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{21}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF1} > P_{12}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{22}$, "okay", "not okay") = "okay"

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

$$H_w := 10.3 \cdot ft$$

Depth of the bore below groundwater elevation

$$H_c := 40.0 \cdot ft$$

Vertical separation distance between critical structure and pipe (Route 9)

$$\gamma := 125 \cdot pcf$$

Assumed unit weight silty sand (B-198.9-1 and SC-1A, ~3+00)

$$\gamma_w := 62.4 \cdot pcf$$

Unit weight of water

$$\gamma' := \gamma - \gamma_w = 62.6 \cdot pcf$$

Effective unit weight

$$u := \gamma_w \cdot H_w = 4 \cdot psi$$

Initial pore water pressure

$$\phi := 34 \cdot deg$$

Assumed friction Angle (KIE)

$$c := 0 \cdot psf = 0 \cdot psi$$

Assumed cohesion of encountered material

$$R_0 := \frac{D_{rod}}{2} = 1.75 \cdot in$$

Initial radius of the borehole

$$R_{pmax} := \frac{2}{3} \cdot H_c = 27 \cdot ft$$

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 30.3 \cdot psi$$

Initial effective stress (conservative assume all buoyant)

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 7 \cdot \frac{N}{mm^2} = 1015 \cdot psi$$

Assumed modulus of elasticity (silty sand)

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 - 0.5
Clay (unsaturated)	0.1 - 0.3
Sandy clay	0.2 - 0.3
Silt	0.3 - 0.35
Sand (dense)	0.2 - 0.4
Course (void ratio = 0.4 - 0.7)	0.15
Fine grained (void ratio = 0.4 - 0.7)	0.25
Rock	0.1 - 0.4 (depends on type of rock)
Loess	0.1 - 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.25$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 406 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot \cos(\phi))}{G} = 0.0417$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 47.2 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot \cot(\phi))) \cdot \left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot \cot(\phi) = 147.5 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 151.9 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$h := 18.04 \text{ ft}$$

Elevation difference between level of bore hole front and structure point of mud flow

$$\gamma_m = 90 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 11.3 \text{ psi}$$

Minimum required mud pressure to overcome differntial head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$v := \frac{Q_f}{0.785 (D_0^2 - D_{PT}^2)} = 75.2 \frac{\text{ft}}{\text{min}}$$

Computed mud flow velocity

$$L_{structure} := 300 \text{ ft}$$

Length to structure

$$p_2 := L_{structure} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 0.9 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 12.2 \text{ psi}$$

Minimum required mud pressure

$$check := \text{if}(p_{max} > p_{min.}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 40 \text{ ft}$$

$$\phi = 34 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 125 \text{ pcf}$$

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} = 0.079$$

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 1 \text{ psi} \quad P_E = 199 \text{ psf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Arching factor (Eq. 6, p.432, PPI)

Effective overburden pressure

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 0.2\%$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 0.4\%$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 90 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \frac{\text{in}^4}{\text{in}}$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.1\%$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for
PE4710, Base Temperature of 73
Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in
borehole (Slurry unit weight)

Moment of inertia of pipe wall cross
section

Pipe ring deflection to buoyant force
ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at
short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_short} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at
long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_long} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 0.2\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 0.4\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

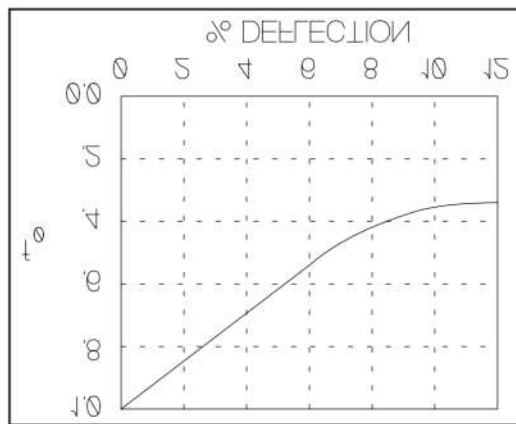
D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$



Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.98$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 125.4 \text{ psi} \quad \text{Allowable unconstrained buckling pressure}$$

$$H = 18 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 11.25 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 11.25 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{long} := 0.45$$

Factor of Safety

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 50 years of sustained loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure 3 (PPI Chp. 12). Use deflection limit calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling pressure

$$P_{GW} := \gamma_w \cdot H_w = 4.463 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

91.A

Defining Parameters of Horizontal Directional Drilling :

$$D_1 := 10.75 \text{ in}$$

Pipe 1 outer diameter

$$D_2 := 2.375 \text{ in}$$

Pipe 2 outer diameter

$$D_{rod} := 3.5 \text{ in}$$

Assumed drill rod diameter

$$DR_1 := 9$$

Dimension ratio of Pipe 1

$$DR_2 := 11$$

Dimension ratio of Pipe 2

$$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$$

Thickness of Pipe 1

$$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$$

Thickness of Pipe 2

$$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$$

Pipe circumference of pipe 1

$$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$$

Pipe circumference of pipe 2

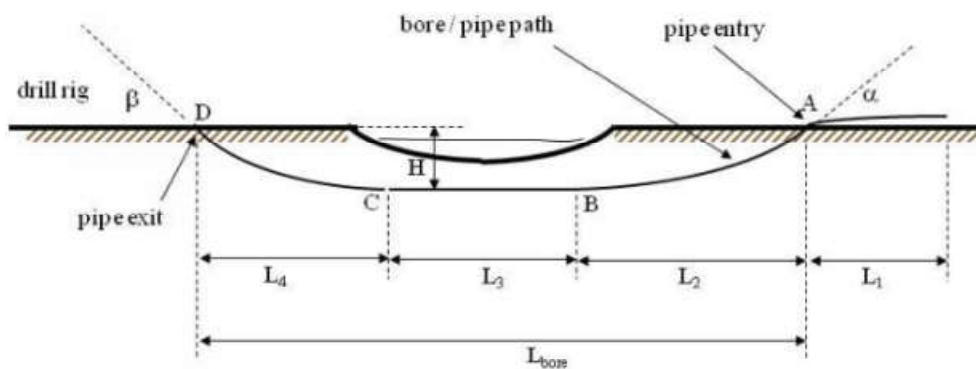


Illustration 1 - Schematic of Drive Cross-section

$$\alpha := 8^\circ$$

$$\alpha_{in} := \alpha = 0.1396 \text{ rad}$$

Borehole entry angle (degrees, radians)

$$\beta := 10^\circ$$

$$\beta_{exit} := \beta = 0.1745 \text{ rad}$$

Borehole exit angle (degrees, radians)

$$D_r := 18 \text{ in}$$

Final reamed bore diameter

$$H_{max} := 23.2 \text{ ft}$$

Max depth of bore hole to final reamed bore diameter

$$H_{max1} := H_{max} + \frac{D_r}{2} = 23.95 \text{ ft}$$

Max depth to bore hole springline from ground surface

$$L_{total} := 1610.6 \text{ ft}$$

Total length of HDD crossing

$$L_1 := 150 \text{ ft}$$

Assumed pipe drag on surface, See Illustration 1

$$L_2 := 218.9 \text{ ft}$$

Horizontal length to achieve depth - provided by Contractor, See Illustration 1

$$L_3 := 1160 \text{ ft}$$

Straight horizontal section

$$L_4 := 231.7 \text{ ft}$$

Horizontal distance to rise to surface, See Illustration 1

$$H := 26.9 \text{ ft}$$

Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 67 \text{ pcf} = 9 \frac{\text{lb}_f}{\text{gal}}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.1$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 36 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1480 \text{ lbf} \quad \text{Pullback force when pipe enters the ground}$$

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} \left(T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})} \right) = 5071 \text{ lbf} \quad \text{Pullback force increase with depth}$$

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 16584 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 19905 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 20701 \text{ lbf} \quad \text{Maximum Pullback Force}$$

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 10.2 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1480 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} (T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 2675 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 5191 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 6005 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 6005 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 19898 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 803 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 5772 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 233 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

check := if ($P_{SPF1} > P_{11}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{21}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF1} > P_{12}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{22}$, "okay", "not okay") = "okay"

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

$$H_w := 19.7 \text{ ft}$$

Depth of the bore below groundwater elevation

$$H_c := 25.1 \text{ ft}$$

Vertical separation distance between critical structure and pipe (Old Ravena Rd., ~8+00)

$$\gamma := 100 \text{ pcf}$$

Assumed unit weight soft to clay/silt (zero blow count clay)

$$\gamma_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma' := \gamma - \gamma_w = 37.6 \text{ pcf}$$

Effective unit weight

$$u := \gamma_w \cdot H_w = 9 \text{ psi}$$

Initial pore water pressure

$$\phi := 0 \text{ deg}$$

Assumed friction Angle

$$c := 450 \text{ psf} = 3.13 \text{ psi}$$

Assumed cohesion of encountered material

$$R_0 := \frac{D_{rod}}{2} = 1.75 \text{ in}$$

Initial radius of the borehole

$$R_{pmax} := \frac{1}{2} \cdot H_c = 13 \text{ ft}$$

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 9 \text{ psi}$$

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 2 \frac{N}{mm^2} = 290 \text{ psi}$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 - 0.5
Clay (unsaturated)	0.1 - 0.3
Sandy clay	0.2 - 0.3
Silt	0.3 - 0.35
Sand (dense)	0.2 - 0.4
Course (void ratio = 0.4 - 0.7)	0.15
Fine grained (void ratio = 0.4 - 0.7)	0.25
Rock	0.1 - 0.4 (depends on type of rock)
Loess	0.1 - 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.5$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 97 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot 0)}{G} = 0$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 12 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max1} := (p'_f + (c \cdot 0)) \cdot \left(\left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot 0 = 12 \text{ psi} \right.$$

$$p'_{max2} := p'_f + c = 15.1 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max2} = 23.7 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$h := 26.9 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 67 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 12.5 \text{ psi}$$

Minimum required mud pressure to overcome differential head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$v := \frac{Q_f}{0.785 (D_r^2 - (D_1^2 + D_2^2))} = 24.2 \frac{ft}{min}$$

Computed mud flow velocity

$$L_{structure} := 800 \text{ ft}$$

Length to structure

$$p_2 := L_{structure} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 2.4 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 14.9 \text{ psi}$$

Minimum required mud pressure

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 23.2 \text{ ft}$$

$$\phi = 0 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 100 \text{ pcf}$$

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} \quad k := 1$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Arching factor (Eq. 6, p.432, PPI)

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 6 \text{ psi} \quad P_E = 872 \text{ psf}$$

Effective overburden pressure

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 0.8\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 1.6\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 67 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \frac{\text{in}^4}{\text{in}}$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.0$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for PE4710, Base Temperature of 73 Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in borehole (Slurry unit weight)

Moment of inertia of pipe wall cross section

Pipe ring deflection to buoyant force ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{short}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{long}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 0.9\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 1.6\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

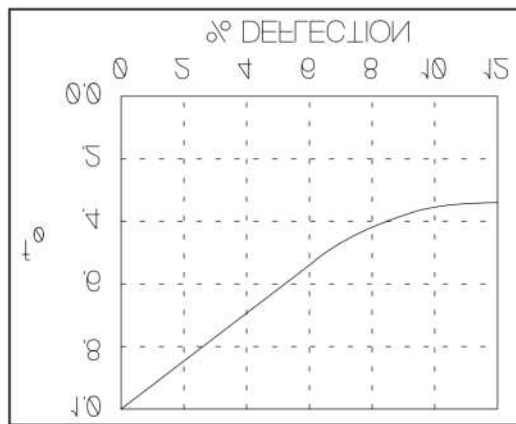
D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$



Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.98$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 125.4 \text{ psi} \quad \text{Allowable unconstrained buckling pressure}$$

$$H = 26.9 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 12.52 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 12.52 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{long} := 0.45$$

Factor of Safety

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 50 years of sustained
loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure
3 (PPI Chp. 12). Use deflection limit
calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling
pressure

$$P_{GW} := \gamma_w \cdot H_w = 8.5 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

92 & 92.A

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

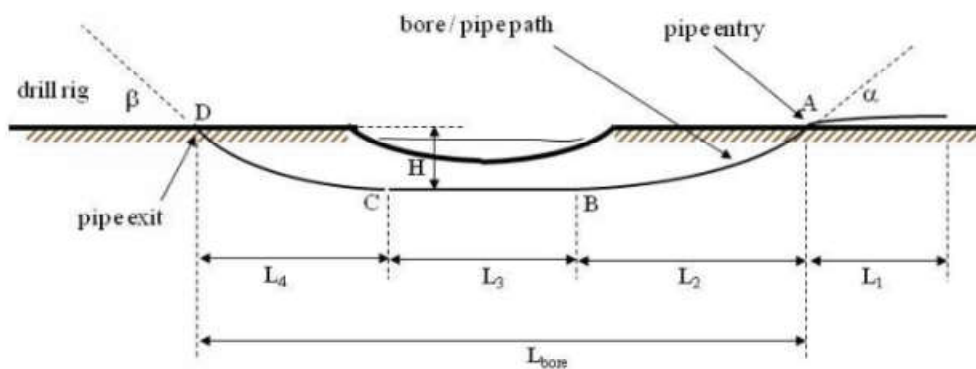


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 12^\circ$	$\alpha_{in} := \alpha = 0.2094 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 12^\circ$	$\beta_{exit} := \beta = 0.2094 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \text{ in}$		Final reamed bore diameter
$H_{max} := 147.6 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 148.35 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 2092 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 702.5 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_3 := 1058 \text{ ft}$		Straight horizontal section
$L_4 := 331 \text{ ft}$		Horizontal distance to rise to surface, See Illustration 1
$H := 50 \text{ ft}$		Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 90 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.4$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 51.2 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1897 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} \left(T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})} \right) = 22193 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 37494 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 45035 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 45831 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 24.6 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1897 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} \left(T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})} \right) = 12058 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 18927 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 22456 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 22456 \text{ lbf} \quad \text{Maximum Pullback Force}$$

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 44053 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 1778 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 21585 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 871 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

$$check := \text{if}(P_{SPF1} > P_{11}, \text{"okay"}, \text{"not okay"}) = \text{"not okay"}$$

$$check := \text{if}(P_{SPF2} > P_{21}, \text{"okay"}, \text{"not okay"}) = \text{"not okay"}$$

$$check := \text{if}(P_{SPF1} > P_{12}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$check := \text{if}(P_{SPF2} > P_{22}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

The first two checks indicate pullback will not be sufficient w/o ballast - therefore, KUE recommends ballast for HDD C1 & C2 (i.e. last two checks are sufficient w/ ballast).

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

- Diameter/radius based on the most critical stage (i.e. during pilot tube)

-Assume $\cot(0 \text{ deg}) = 0$ theoretically infinite)

$$D_{PT} := 5 \text{ in}$$

$$D_0 := 9.5 \text{ in}$$

$$H_m := 18.9 \text{ ft}$$

$$H_c := 18.9 \text{ ft}$$

$$\gamma := 100 \text{ pcf}$$

$$\gamma_w := 62.4 \text{ pcf}$$

$$\gamma' := \gamma - \gamma_w = 37.6 \text{ pcf}$$

$$u := \gamma_w \cdot H_m = 8.2 \text{ psi}$$

$$\phi := 0 \text{ deg}$$

$$c := 450 \text{ psf} = 3.13 \text{ psi}$$

$$R_0 := \frac{D_0}{2} = 4.75 \text{ in}$$

$$R_{pmax} := \frac{1}{2} \cdot H_c = 9.5 \text{ ft}$$

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 4.9 \text{ psi}$$

Pilot tube diameter

Initial borehole diameter for pilot tube

Depth of the bore below groundwater El.

Vertical separation distance between critical structure and pipe (S-14)

Assumed unit weight soft clay/silt (CL-ML)

Unit weight of water

Effective unit weight

Initial pore water pressure

Assumed friction Angle

Assumed cohesion of encountered material

Initial radius of the borehole

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 5 \frac{\text{N}}{\text{mm}^2} = 725 \text{ psi}$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 - 0.5
Clay (unsaturated)	0.1 - 0.3
Sandy clay	0.2 - 0.3
Silt	0.3 - 0.35
Sand (dense)	0.2 - 0.4
Course (void ratio = 0.4 - 0.7)	0.15
Fine grained (void ratio = 0.4 - 0.7)	0.25
Rock	0.1-0.4 (depends on type of rock)
Loess	0.1 - 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.4$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 259 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot 0)}{G} = 0$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 8.1 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot Q)) \cdot \left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot 0 = 8.1 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 16.3 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$h := 106.5 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 90 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 66.6 \text{ psi}$$

Minimum required mud pressure to overcome differential head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$v := \frac{Q_f}{0.785 (D_0^2 - D_{PT}^2)} = 75.2 \frac{\text{ft}}{\text{min}}$$

Computed mud flow velocity

$$v = 1.3 \frac{ft}{s}$$

Computed mud flow velocity (check on units)

$$L_{structure} := 1825 \text{ ft}$$

Length to structure

$$\left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 0.003 \frac{psi}{ft} \quad \text{Check mud pressure units}$$

$$p_2 := L_{structure} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 5.5 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 72 \text{ psi}$$

Minimum required mud pressure

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 147.6 \text{ ft}$$

$$\phi = 0 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2 = 2.624$$

$$\gamma = 100 \text{ pcf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Can't divide by 0 ~ assume friction angle (ϕ) = 1×10^{-2}

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot 1 \cdot 10^{-2}\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot 1 \cdot 10^{-2}} = 0.193$$

Arching factor (Eq. 6, p.432, PPI)

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 7 \text{ psi} \quad P_E = 1069 \text{ psf} \text{ Effective overburden pressure}$$

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

$$k := 1$$

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

Variable in earth load deflection equation

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 1.0\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

Variable in earth load deflection equation

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 2.0\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 90 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \text{ in}^4$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.1\%$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for PE4710, Base Temperature of 73 Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in borehole (Slurry unit weight)

Moment of inertia of pipe wall cross section

Pipe ring deflection to buoyant force ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{short}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{long}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 1.1\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 2.0\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

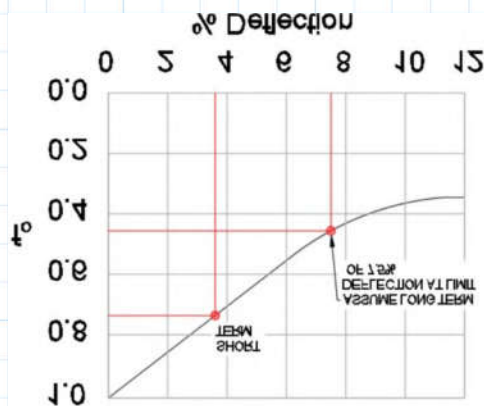
D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$



Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.75$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 96 \text{ psi}$$

Allowable unconstrained buckling pressure

$$H = 50 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 31.25 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 31.25 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

Factor of Safety

$$\mu_{long} := 0.45$$

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 50 years of sustained loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure 3 (PPI Chp. 12). Use deflection limit calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling pressure

$$P_{GW} := \gamma_w \cdot H_w = 8.19 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

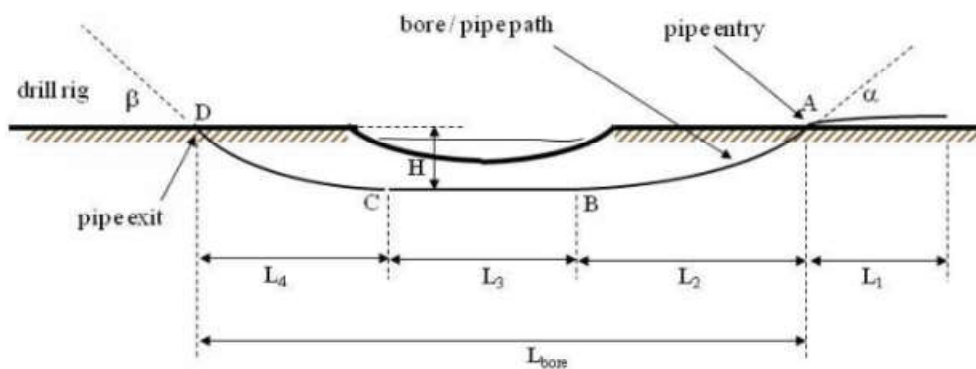


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 9^\circ$	$\alpha_{in} := \alpha = 0.1571 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 10^\circ$	$\beta_{exit} := \beta = 0.1745 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \text{ in}$		Final reamed bore diameter
$H_{max} := 27.3 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 28.05 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 1666.6 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 221.8 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_3 := 1249 \text{ ft}$		Straight horizontal section
$L_4 := 195.8 \text{ ft}$		Horizontal distance to rise to surface, See Illustration 1
$H := 16.8 \text{ ft}$		Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 90 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.4$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 51.2 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1529 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 6445 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 24530 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - w_b \cdot H_{max} - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 27369 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 28165 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 24.6 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1529 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} (T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 4223 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 12356 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 14370 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 14370 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 27073 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 1093 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 13812 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 557 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

check := if ($P_{SPF1} > P_{11}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{21}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF1} > P_{12}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{22}$, "okay", "not okay") = "okay"

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

- Diameter/radius based on the most critical stage (i.e. during pilot tube)

-Assume $\cot(0 \text{ deg}) = 0$ theoretically infinite)

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$H_w := 17.4 \text{ ft}$$

Depth of the bore below groundwater elevation

$$H_c := 17.4 \text{ ft}$$

Vertical separation distance between critical structure and pipe (wetlands; ~Sta 5+50)

$$\gamma := 110 \text{ pcf}$$

Assumed unit weight med stiff to stiff silty clay & silt (ML, CL-ML)

$$\gamma_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma' := \gamma - \gamma_w = 47.6 \text{ pcf}$$

Effective unit weight

$$u := \gamma_w \cdot H_w = 7.5 \text{ psi}$$

Initial pore water pressure

$$\phi := 0 \text{ deg}$$

Assumed friction Angle

$$c := 800 \text{ psf} = 5.56 \text{ psi}$$

Assumed cohesion of encountered material

$$R_0 := \frac{D_{rod}}{2} = 1.75 \text{ in}$$

Initial radius of the borehole

$$R_{pmax} := \frac{1}{2} \cdot H_c = 9 \text{ ft}$$

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 5.8 \text{ psi}$$

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 15 \frac{\text{N}}{\text{mm}^2} = 2176 \text{ psi}$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 - 0.5
Clay (unsaturated)	0.1 - 0.3
Sandy clay	0.2 - 0.3
Silt	0.3 - 0.35
Sand (dense)	0.2 - 0.4
Course (void ratio = 0.4 - 0.7)	0.15
Fine grained (void ratio = 0.4 - 0.7)	0.25
Rock	0.1 - 0.4 (depends on type of rock)
Loess	0.1 - 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.4$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 777 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot 0)}{G} = 0$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 11.3 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot 0)) \cdot \left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot 0 = 11.3 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 18.8 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$h := 16.85 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 90 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 10.5 \text{ psi}$$

Minimum required mud pressure to overcome differential head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$v := \frac{Q_f}{0.785 (D_0^2 - D_{PT}^2)} = 75.2 \frac{\text{ft}}{\text{min}}$$

Computed mud flow velocity

$$L_{structure} := 550 \text{ ft}$$

Length to structure

$$\left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 0.003 \frac{\text{psi}}{\text{ft}} \quad \text{Check mud pressure units}$$

$$p_2 := L_{structure} \cdot \left(\left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) \right) = 1.6 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 12.2 \text{ psi}$$

Minimum required mud pressure

$$check := \text{if}(p_{max} > p_{min.}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 27.3 \text{ ft}$$

$$\phi = 0 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 110 \text{ pcf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Can't divide by 0 ~ assume k goes to 1 (ie full soil column height)

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} \quad k := 1 \quad \text{Arching factor (Eq. 6, p.432, PPI)}$$

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 9 \text{ psi} \quad P_E = 1299 \text{ psf} \quad \text{Effective overburden pressure}$$

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 1.2\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 2.5\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 90 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \text{ in}^4$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.1\%$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for PE4710, Base Temperature of 73 Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in borehole (Slurry unit weight)

Moment of inertia of pipe wall cross section

Pipe ring deflection to buoyant force ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_short} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_long} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 1.3\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 2.5\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

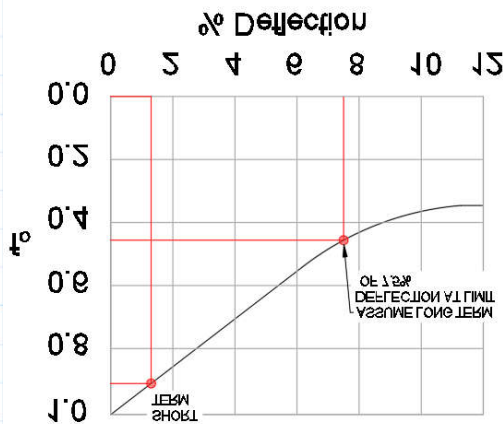
$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$

Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)



Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.92$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 117.7 \text{ psi}$$

Allowable unconstrained buckling pressure

$$H = 16.8 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 10.5 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 10.5 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

Factor of Safety

$$\mu_{long} := 0.45$$

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 50 years of sustained
loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure
3 (PPI Chp. 12). Use deflection limit
calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling
pressure

$$P_{GW} := \gamma_w \cdot H_w = 7.54 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

93.A

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

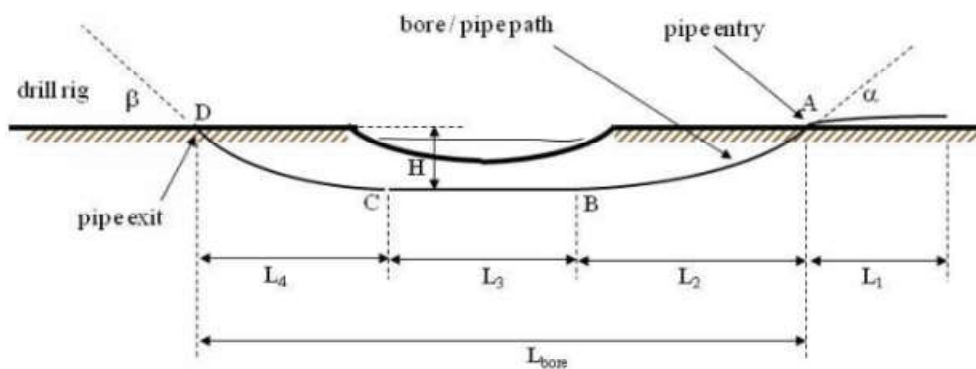


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 10^\circ$	$\alpha_{in} := \alpha = 0.1745 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 14^\circ$	$\beta_{exit} := \beta = 0.2443 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \text{ in}$		Final reamed bore diameter
$H_{max} := 44.7 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 45.45 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 744.0 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 370.1 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_3 := 70.6 \text{ ft}$		Straight horizontal section
$L_4 := 296.5 \text{ ft}$		Horizontal distance to rise to surface, See Illustration 1
$H := 44.3 \text{ ft}$		Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 80 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.3$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 44.6 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 748 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 7778 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 8660 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - w_b \cdot H_{max} - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 11168 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 11965 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 18.3 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 748 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} (T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 4128 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 4453 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 6274 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 6274 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 11500 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 464 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 6031 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 243 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

check := if ($P_{SPF1} > P_{11}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{21}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF1} > P_{12}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{22}$, "okay", "not okay") = "okay"

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

-Assume soil conditions of soft clay (CL), B202.1-1 does not extend to bottom tangent of HDD alignment.

- Diameter/radius based on the most critical stage (i.e. during pilot tube)

-Assume $\cot(0 \text{ deg}) = 0$ theoretically infinite)

$$D_{PT} := 5 \text{ in}$$

$$D_0 := 9.5 \text{ in}$$

$$H_w := 26.1 \text{ ft}$$

$$H_c := 26.1 \text{ ft}$$

$$\gamma := 110 \text{ pcf}$$

$$\gamma_w := 62.4 \text{ pcf}$$

$$\gamma' := \gamma - \gamma_w = 47.6 \text{ pcf}$$

$$u := \gamma_w \cdot H_w = 11 \text{ psi}$$

$$\phi := 0 \text{ deg}$$

$$c := 800 \text{ psf} = 5.56 \text{ psi}$$

$$R_0 := \frac{D_{rod}}{2} = 1.75 \text{ in}$$

$$R_{pmax} := \frac{1}{2} \cdot H_c = 13 \text{ ft}$$

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 9 \text{ psi}$$

Pilot tube diameter

Initial borehole diameter for pilot tube

Depth of the bore below groundwater elevation

Vertical separation distance between critical structure and pipe (Stream, ~2+25)

Assumed unit weight soft clay

Unit weight of water

Effective unit weight

Initial pore water pressure

Assumed friction Angle

Assumed cohesion of encountered material

Initial radius of the borehole

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 15 \frac{N}{mm^2} = 2176 \text{ psi}$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 - 0.5
Clay (unsaturated)	0.1 - 0.3
Sandy clay	0.2 - 0.3
Silt	0.3 - 0.35
Sand (dense)	0.2 - 0.4
Course (void ratio = 0.4 - 0.7)	0.15
Fine grained (void ratio = 0.4 - 0.7)	0.25
Rock	0.1 - 0.4 (depends on type of rock)
Loess	0.1 - 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.4$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 777 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot 0)}{G} = 0$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 14.2 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot 0)) \cdot \left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot 0 = 14.2 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 25.5 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$h := 41.4 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 80 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 23 \text{ psi}$$

Minimum required mud pressure to overcome differntial head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$v := \frac{Q_f}{0.785 (D_0^2 - D_{PT}^2)} = 75.2 \frac{\text{ft}}{\text{min}}$$

Computed mud flow velocity

$$L_{structure} := 225 \text{ ft}$$

Length to structure

$$\left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 0.003 \frac{\text{psi}}{\text{ft}} \quad \text{Check mud pressure units}$$

$$p_2 := L_{structure} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 0.7 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 23.7 \text{ psi}$$

Minimum required mud pressure

$$check := \text{if}(p_{max} > p_{min.}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 44.7 \text{ ft}$$

$$\phi = 0 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 110 \text{ pcf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Can't divide by 0 ~ assume k goes to 1 (ie full soil column height)

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} \quad k := 1 \quad \text{Arching factor (Eq. 6, p.432, PPI)}$$

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 15 \text{ psi} \quad P_E = 2128 \text{ psf} \quad \text{Effective overburden pressure}$$

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 2.0\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

Variable in earth load deflection equation

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 4.0\%$$

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 80 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \text{ in}^4$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.1\%$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for
PE4710, Base Temperature of 73
Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in
borehole (Slurry unit weight)

Moment of inertia of pipe wall cross
section

Pipe ring deflection to buoyant force
ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at
short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_short} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at
long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_long} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 2.0\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 4.0\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

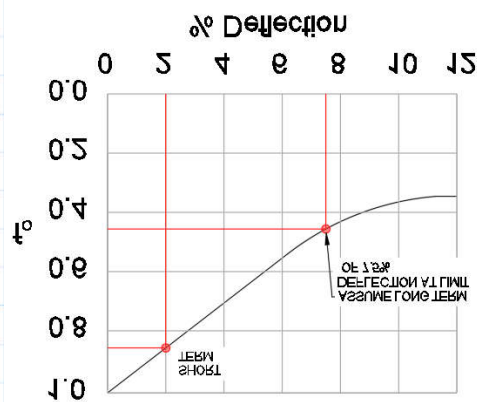
$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$

Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)



Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.87$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 111.3 \text{ psi} \quad \text{Allowable unconstrained buckling pressure}$$

$$H = 44.3 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 24.61 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 24.61 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{long} := 0.45$$

Factor of Safety

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 50 years of sustained loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure 3 (PPI Chp. 12). Use deflection limit calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling pressure

$$P_{GW} := \gamma_w \cdot H_w = 11.31 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

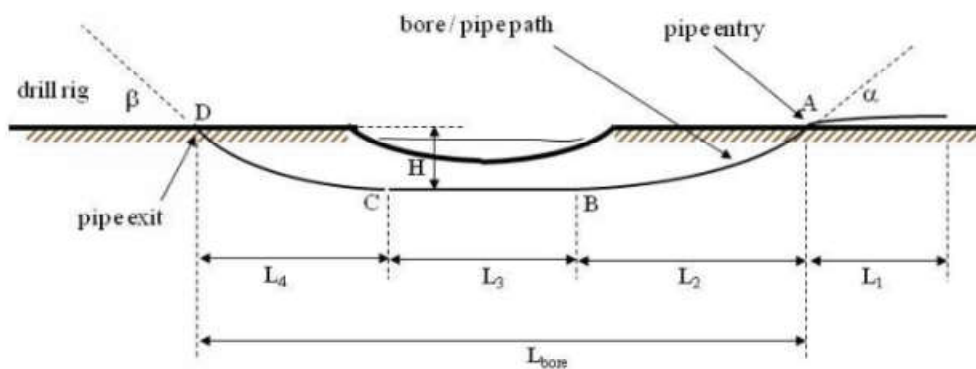


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 8^\circ$	$\alpha_{in} := \alpha = 0.1396 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 10^\circ$	$\beta_{exit} := \beta = 0.1745 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \text{ in}$		Final reamed bore diameter
$H_{max} := 43.3 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 44.05 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 1176.5 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 234.6 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_{3_1} := 174.6 \text{ ft}$		Straight horizontal section, before curve
$L_{3_2} := 32.9 \text{ ft}$		Curve Length
$L_{3_3} := 127.9 \text{ ft}$		Straight horizontal section, after curve

$$L_4 := 285.9 \text{ ft}$$

Horizontal distance to rise to surface, See Illustration 1

$$H := 32 \text{ ft}$$

Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters (rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 90 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.4$$

Specific gravity of slurry, assumed unit weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 51.2 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_{3-1} + L_{3-2} + L_{3-3} + L_4)) = 845 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} \cdot (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 6746 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C1:

$$T_{c-1} := T_b + (v_b \cdot w_b \cdot L_{3-1}) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_{3-1} \cdot e^{(v_a \cdot \alpha_{in})}) = 9276 \text{ lbf}$$

B1.7 - Pullback Force Point C2:

$$\alpha_{curve} := 18.9^\circ$$

$$T_{c-2} := e^{v_b \cdot \alpha_{curve}} \cdot (T_{c-1} + v_b \cdot |w_b| \cdot L_{3-2} + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_{3-2} \cdot e^{(v_a \cdot \alpha_{curve})}) = 13215 \text{ lbf}$$

B1.8 - Pullback Force Point C3:

$$T_{c-3} := T_{c-2} + (v_b \cdot w_b \cdot L_{3-3}) - e^{(v_b \cdot \alpha_{curve})} \cdot (v_a \cdot w_a \cdot L_{3-3} \cdot e^{(v_a \cdot \alpha_{curve})}) = 15059 \text{ lbf}$$

B1.9 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{exit})} \cdot (T_{c-3} + v_b \cdot |w_b| \cdot L_4 - w_b \cdot H_{max} - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 17904 \text{ lbf}$$

B1.10 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_{c-1}, T_{c-2}, T_{c-3}, T_d) + \Delta T = 18700 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 24.6 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_{3_1} + L_{3_2} + L_{3_3} + L_4)) = 845 \text{ lbf}$$

Pullback force enter ground

B2.3 - Pullback Force Point B:

$$T_{b\text{filled}} := e^{v_b \cdot \alpha_{in}} (T_{a\text{filled}} + v_b \cdot |w_{b\text{filled}}| \cdot L_2 + w_{b\text{filled}} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 4009 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C1:

$$T_{c1_filled} := T_{b\text{filled}} + (v_b \cdot |w_{b\text{filled}}| \cdot L_{3_1}) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_{3_1} \cdot e^{(v_a \cdot \alpha_{in})}) = 5147 \text{ lbf}$$

B2.5 - Pullback Force Point C2:

$$\alpha_{curve} = 18.9^\circ$$

$$T_{c2_filled} := e^{v_b \cdot \alpha_{curve}} (T_{c1_filled} + v_b \cdot |w_{b\text{filled}}| \cdot L_{3_2} + w_{b\text{filled}} \cdot H_{max} + v_a \cdot w_a \cdot L_{3_2} \cdot e^{(v_a \cdot \alpha_{curve})}) = 7160 \text{ lbf}$$

B2.6 - Pullback Force Point C3:

$$T_{c3_filled} := T_{c2_filled} + (v_b \cdot |w_{b\text{filled}}| \cdot L_{3_3}) - e^{(v_b \cdot \alpha_{curve})} \cdot (v_a \cdot w_a \cdot L_{3_1} \cdot e^{(v_a \cdot \alpha_{curve})}) = 7941 \text{ lbf}$$

B2.7 - Pullback Force at D:

$$T_{d\text{filled}} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{c3_filled} + v_b \cdot |w_{b\text{filled}}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 10338 \text{ lbf}$$

B2.8 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{a\text{filled}}, T_{b\text{filled}}, T_{c1_filled}, T_{c2_filled}, T_{c3_filled}, T_{d\text{filled}}) = 10338 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 17975 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 726 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 9937 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 401 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

$check := \text{if}(P_{SPF1} > P_{11}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$

$check := \text{if}(P_{SPF2} > P_{21}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$

$check := \text{if}(P_{SPF1} > P_{12}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$

$check := \text{if}(P_{SPF2} > P_{22}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

- Geologic conditions through alignment will vary from very poor (inferred from weathered rock) to fair rock mass quality based on Boring K204.2. Assume critical section is silty sand based on boring K-203.5 & -.6 for Mathcad.

$$H_w := 16.5 \cdot ft$$

Depth of the bore below groundwater elevation

$$H_c := 27 \cdot ft$$

Vertical separation distance between critical structure and pipe (Main St)

$$\gamma := 125 \cdot pcf$$

Assumed unit weight silty sand (SM)

$$\gamma_w := 62.4 \cdot pcf$$

Unit weight of water

$$\gamma' := \gamma - \gamma_w = 62.6 \cdot pcf$$

Effective unit weight

$$u := \gamma_w \cdot H_w = 7 \cdot psi$$

Initial pore water pressure

$$\phi := 34 \cdot deg$$

Assumed friction Angle

$$c := 0 \cdot psf = 0 \cdot psi$$

Assumed cohesion of encountered material

$$R_0 := \frac{D_{rod}}{2} = 1.75 \cdot in$$

Initial radius of the borehole

$$R_{pmax} := \frac{2}{3} \cdot H_c = 18 \cdot ft$$

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 16 \cdot psi$$

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 7 \cdot \frac{N}{mm^2} = 1015 \cdot psi$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 – 0.5
Clay (unsaturated)	0.1 – 0.3
Sandy clay	0.2 – 0.3
Silt	0.3 – 0.35
Sand (dense)	0.2 – 0.4
Course (void ratio = 0.4 – 0.7)	0.15
Fine grained (void ratio = 0.4 – 0.7)	0.25
Rock	0.1–0.4 (depends on type of rock)
Loess	0.1 – 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.25$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 406 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot \cot(\phi))}{G} = 0.0224$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 25.4 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot \cot(\phi))) \cdot \left(\left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot \cot(\phi) \right) = 99 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 106.2 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$h := 23.18 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 90 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 14.5 \text{ psi}$$

Minimum required mud pressure to overcome differntial head

$$Q_f := 200 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 16 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 25 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$D_{eff} := 13.4870 \text{ in}$$

Effective diameter of bundle

$$v := \frac{Q_f}{0.785 \left((D_0^2 - D_{PT}^2) \right)} = 75.2 \frac{ft}{min}$$

Computed mud flow velocity

$$L_{total} := 1176.5 \text{ ft}$$

Total length of HDD crossing

$$p_2 := L_{total} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_r - (D_{eff}))^2} \right) + \left(\frac{\tau_o}{(D_r - (D_{eff}))} \right) \right) = 3.5 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 18 \text{ psi}$$

Minimum required mud pressure

$$check := \text{if } (p_{max} > p_{min.}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 43.3 \text{ ft}$$

$$\phi = 34 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 125 \text{ pcf}$$

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} = 0.073$$

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 1 \text{ psi} \quad P_E = 199 \text{ psf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Arching factor (Eq. 6, p.432, PPI)

Effective overburden pressure

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 0.2\%$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 0.4\%$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 90 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \text{ in}^4$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.1\%$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for PE4710, Base Temperature of 73 Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in borehole (Slurry unit weight)

Moment of inertia of pipe wall cross section

Pipe ring deflection to buoyant force ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_short} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_long} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 0.2\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 0.4\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

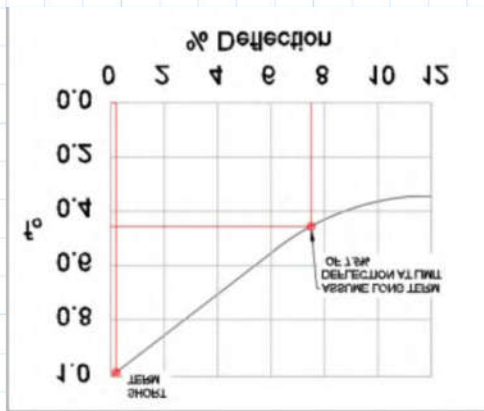
$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$

Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)



Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.98$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 125.4 \text{ psi}$$

Allowable unconstrained buckling pressure

$$H = 32 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 20 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 20 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

Factor of Safety

$$\mu_{long} := 0.45$$

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 50 years of sustained loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.45$$

Ovality compensation factor, Figure 3 (PPI Chp. 12). Use deflection limit calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 31.1 \text{ psi}$$

Allowable unconstrained buckling pressure

$$P_{GW} := \gamma_w \cdot H_w = 7.15 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

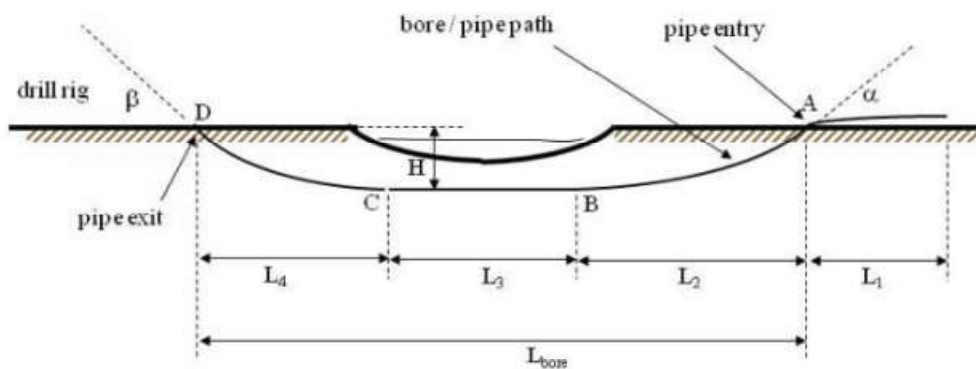


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 10^\circ$	$\alpha_{in} := \alpha = 0.1745 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 10^\circ$	$\beta_{exit} := \beta = 0.1745 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \text{ in}$		Final reamed bore diameter
$H_{max} := 53 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 53.75 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 1241.4 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 472.6 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_{3_1} := 100 \text{ ft}$		Straight horizontal section, before curve
$L_{3_2} := 144.7 \text{ ft}$		Curve Length
$L_{3_3} := 164.5 \text{ ft}$		Straight horizontal section, after curve

$$L_4 := 361.6 \text{ ft}$$

Horizontal distance to rise to surface, See Illustration 1

$$H := 46 \text{ ft}$$

Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters (rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 70 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.1$$

Specific gravity of slurry, assumed unit weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 38 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_{3-1} + L_{3-2} + L_{3-3} + L_4)) = 1175 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 8615 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C1:

$$T_{c-1} := T_b + (v_b \cdot w_b \cdot L_{3-1}) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_{3-1} \cdot e^{(v_a \cdot \alpha_{in})}) = 9666 \text{ lbf}$$

B1.7 - Pullback Force Point C2:

$$\alpha_{curve} := 8.18^\circ$$

$$T_{c-2} := e^{v_b \cdot \alpha_{curve}} (T_{c-1} + v_b \cdot |w_b| \cdot L_{3-2} + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_{3-2} \cdot e^{(v_a \cdot \alpha_{curve})}) = 13784 \text{ lbf}$$

B1.8 - Pullback Force Point C3:

$$T_{c-3} := T_{c-2} + (v_b \cdot w_b \cdot L_{3-3}) - e^{(v_b \cdot \alpha_{curve})} \cdot (v_a \cdot w_a \cdot L_{3-3} \cdot e^{(v_a \cdot \alpha_{curve})}) = 15515 \text{ lbf}$$

B1.9 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{exit})} \cdot (T_{c-3} + v_b \cdot |w_b| \cdot L_4 - w_b \cdot H_{max} - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 18243 \text{ lbf}$$

B1.10 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_{c-1}, T_{c-2}, T_{c-3}, T_d) + \Delta T = 19039 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 12 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot \left(v_a \cdot w_a \cdot (L_1 + L_2 + L_{3_1} + L_{3_2} + L_{3_3} + L_4) \right) = 1175 \text{ lbf}$$

Pullback force enter ground

B2.3 - Pullback Force Point B:

$$T_{b\text{filled}} := e^{v_b \cdot \alpha_{in}} \cdot \left(T_{a\text{filled}} + v_b \cdot |w_{b\text{filled}}| \cdot L_2 + w_{b\text{filled}} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})} \right) = 4130 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C1:

$$T_{c1_filled} := T_{b\text{filled}} + \left(v_b \cdot |w_{b\text{filled}}| \cdot L_{3_1} \right) - e^{(v_b \cdot \alpha_{in})} \cdot \left(v_a \cdot w_a \cdot L_{3_1} \cdot e^{(v_a \cdot \alpha_{in})} \right) = 4402 \text{ lbf}$$

B2.5 - Pullback Force Point C2:

$$\alpha_{curve} = 8.18^\circ$$

$$T_{c2_filled} := e^{v_b \cdot \alpha_{curve}} \cdot \left(T_{c1_filled} + v_b \cdot |w_{b\text{filled}}| \cdot L_{3_2} + w_{b\text{filled}} \cdot H_{max} + v_a \cdot w_a \cdot L_{3_2} \cdot e^{(v_a \cdot \alpha_{curve})} \right) = 5933 \text{ lbf}$$

B2.6 - Pullback Force Point C3:

$$T_{c3_filled} := T_{c2_filled} + \left(v_b \cdot |w_{b\text{filled}}| \cdot L_{3_3} \right) - e^{(v_b \cdot \alpha_{curve})} \cdot \left(v_a \cdot w_a \cdot L_{3_1} \cdot e^{(v_a \cdot \alpha_{curve})} \right) = 6440 \text{ lbf}$$

B2.7 - Pullback Force at D:

$$T_{d\text{filled}} := e^{(v_b \cdot \beta_{exit})} \cdot \left(T_{c3_filled} + v_b \cdot |w_{b\text{filled}}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot \left(v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})} \right) \right) = 7835 \text{ lbf}$$

B2.8 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{a\text{filled}}, T_{b\text{filled}}, T_{c1_filled}, T_{c2_filled}, T_{c3_filled}, T_{d\text{filled}}) = 7835 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} \left(D_1^2 - (D_1 - T_{p1})^2 \right) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} \left(D_2^2 - (D_2 - T_{p2})^2 \right) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 18300 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 739 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 7531 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 304 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

$check := \text{if}(P_{SPF1} > P_{11}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$
 $check := \text{if}(P_{SPF2} > P_{21}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$
 $check := \text{if}(P_{SPF1} > P_{12}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$
 $check := \text{if}(P_{SPF2} > P_{22}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$

C - Allowable Mud Pressures:

C1 - Max. Allowable Drilling Fluid Pressure

Assumptions:

-MathCAD calculations are used for a critical structure as identified for each crossing. If the HDD alignment crosses multiple structures the one with least cover was used. Provided hydrofracture graphs use equations, as detailed herein, to identify potential frac-out areas. Typically entry and exit areas are most susceptible to frac-out due to low cover.

-Where applicable, soil properties referenced from Kiewit's Proposed Soil Properties for CHPE Package 1, dated October 12, 2022.

$$H_w := 0 \text{ ft}$$

Depth of the bore below groundwater elevation

$$H_c := 25.0 \text{ ft}$$

Vertical separation distance between critical structure and pipe (Coyemans Creek)

$$\gamma := 140 \text{ pcf}$$

Assumed unit weight shale bedrock

$$\gamma_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma' := \gamma - \gamma_w = 77.6 \text{ pcf}$$

Effective unit weight

$$u := \gamma_w \cdot H_w = 0 \text{ psi}$$

Initial pore water pressure

$$\phi := 37 \text{ deg}$$

Assumed friction Angle

$$c := 0 \text{ psf} = 0 \text{ psi}$$

Assumed cohesion of encountered material

$$R_0 := \frac{D_{rod}}{2} = 1.75 \text{ in}$$

Initial radius of the borehole

$$R_{pmax} := \frac{2}{3} \cdot H_c = 17 \text{ ft}$$

Radius of plastic zone (H/2 in clays & 2/3 H in sands)

$$\sigma'_0 := ((\gamma \cdot (H_c - H_w)) + \gamma' \cdot H_w) = 24 \text{ psi}$$

Initial effective stress

Table C.2 Typical values of modulus of elasticity (E_s) for different types of soils

Type of Soil	E_s (N/mm ²)
Clay	
Very soft	2-15
Soft	5-25
Medium	15-50
Hard	50-100
Sandy	25-250
Glacial till	
Loose	10-153
Dense	144-720
Very dense	478-1,440
Loess	14-57
Sand	
Silty	7-21
Loose	10-24
Dense	48-81
Sand and gravel	
Loose	48-148
Dense	96-192
Shale	144-14,400
Silt	2-20

$$E_s := 4000 \text{ psi}$$

Assumed modulus of elasticity

Table C.4 Typical values of Poisson's ratio (μ) for soils

Type of soil	μ
Clay (saturated)	0.4 – 0.5
Clay (unsaturated)	0.1 – 0.3
Sandy clay	0.2 – 0.3
Silt	0.3 – 0.35
Sand (dense)	0.2 – 0.4
Course (void ratio = 0.4 – 0.7)	0.15
Fine grained (void ratio = 0.4 – 0.7)	0.25
Rock	0.1–0.4 (depends on type of rock)
Loess	0.1 – 0.3
Ice	0.36
Concrete	0.15

$$\nu_s := 0.4$$

Poissons ratio of material encountered

$$G := \frac{E_s}{2(1 + \nu_s)} = 1429 \text{ psi}$$

Shear modulus of soil

$$Q := \frac{(\sigma'_0 \cdot \sin(\phi)) + (c \cdot \cot(\phi))}{G} = 0.0102$$

Coefficient of Delft Equation

$$p'_f := \sigma'_0 \cdot (1 + \sin(\phi)) + c \cdot \cos(\phi) = 38.9 \text{ psi}$$

Mud pressure at which the first plastic deformation takes place

$$p'_{max} := (p'_f + (c \cdot \cot(\phi))) \cdot \left(\left(\left(\frac{R_0}{R_{pmax}} \right)^2 + Q \right)^{\left(\frac{-\sin(\phi)}{1 + \sin(\phi)} \right)} - c \cdot \cot(\phi) \right) = 217.1 \text{ psi}$$

Maximum allowable effective mud pressure (Delft Equation)

$$p_{max} := u + p'_{max} = 217.1 \text{ psi}$$

Maximum allowable mud pressure

C2 -Min. Allowable Drilling Fluid Pressure

$$D_{PT} := 5 \text{ in}$$

Pilot tube diameter

$$D_0 := 9.5 \text{ in}$$

Initial borehole diameter for pilot tube

$$h := 48.85 \text{ ft}$$

Elevation difference between level of bore hole front and exit point of mud flow

$$\gamma_m = 70 \text{ pcf}$$

Unit weight of slurry/mud

$$p_1 := \gamma_m \cdot h = 23.7 \text{ psi}$$

Minimum required mud pressure to overcome differntial head

$$Q_f := 80 \text{ gpm}$$

Assumed mud flow rate

$$\tau_o := 25 \frac{\text{lbf}}{100 \cdot \text{ft}^2}$$

Assumed yield point of mud per 100 square feet

$$\mu_{pl} := 72 \cdot \frac{\text{poise}}{100}$$

Assumed plastic viscosity of mud

$$D_{eff} := 13.4870 \text{ in}$$

Effective diameter of bundle

$$v := \frac{Q_f}{0.785 \left((D_0^2 - D_{PT}^2) \right)} = 30.1 \frac{\text{ft}}{\text{min}}$$

Computed mud flow velocity

$$L_{total} = 1241.4 \text{ ft}$$

Length of bore

$$p_2 := L_{total} \cdot \left(\left(\frac{\mu_{pl} \cdot v}{(D_0 - D_{PT})^2} \right) + \left(\frac{\tau_o}{(D_0 - D_{PT})} \right) \right) = 5.8 \text{ psi}$$

Minimum required mud pressure to create flow inside the borehole

$$p_{min.} := p_1 + p_2 = 29.5 \text{ psi}$$

Minimum required mud pressure

$$check := \text{if}(p_{max} > p_{min.}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D - Pipe Structural Capacities:

D1- Ring Deflection (Short & Long Term):

D1.1 - Overburden Pressure (Considering Deformed Borehole with Arching Mobilized)

$$H_c := H_{max} = 53 \text{ ft}$$

$$\phi = 37 \text{ deg}$$

$$B := D_r = 18 \text{ in}$$

$$K := \tan\left(45 - \frac{\phi}{2}\right)^2$$

$$\gamma = 140 \text{ pcf}$$

$$k := \frac{1 - \exp\left(-2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)\right)}{2 \cdot \frac{K \cdot H_c}{B} \cdot \tan\left(\frac{\phi}{2}\right)} = 0.061$$

$$P_E := k \cdot (\gamma - \gamma_w) \cdot (H_c) = 2 \text{ psi} \quad P_E = 250 \text{ psf}$$

Depth of cover

Friction angle of soil

"Silo" width, conservative value =
reamed hole diameter

Earth pressure coefficient

Unit weight of soil, assumed

Arching factor (Eq. 6, p.432, PPI)

Effective overburden pressure

D1.2 Earth Load Deflection (Short Term)

$$E_{short} := 57500 \cdot \text{psi}$$

$$k_{short} := \frac{E_{short}}{12 \cdot (DR_1 - 1)^3} = 9.36 \text{ psi}$$

$$\Delta y_{ELD_short} := \frac{0.0125 \cdot P_E}{k_{short}} = 0.2\%$$

Apparent modulus of elasticity for
PE4710, Base Temperature of 73 deg.
Fahrenheit at 10 hrs of sustained loading
(Table X1.1 ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437, PPI Handbook)

D1.3 Earth Load Deflection (Long Term)

$$E_{long} := 28200 \cdot \text{psi}$$

$$k := \frac{E_{long}}{12 \cdot (DR_1 - 1)^3} = 4.6 \text{ psi}$$

$$\Delta y_{ELD_long} := \frac{0.0125 \cdot P_E}{k} = 0.5\%$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 Fahrenheit at 50
years of sustained loading (Table X1.1
ASTM F 1962)

Variable in earth load deflection equation

Pipe deflection to diameter as per
PPI Equ. 10 (Chp 12, p 437)

D2 - Buoyant Deflection

D2.1 Buoyant Deflection (Short Term)

$$D_1 = 10.75 \text{ in}$$

$$t := T_{p1} = 1.194 \text{ in}$$

$$E_{short} = 57500 \text{ psi}$$

$$\gamma_m = 70 \text{ pcf}$$

$$I := \frac{t^3}{12} = 0.14 \text{ in}^4$$

$$\Delta y_{buoyant} := \frac{0.1169 \cdot \gamma_m \cdot \left(\frac{D_1}{2}\right)^4}{E_{short} \cdot I} = 0.0$$

Outside diameter of casing pipe

Thickness of casing pipe

Apparent modulus of elasticity for
PE4710, Base Temperature of 73
Fahrenheit (Table B.1.1)

Assumed unit weight of fluid in
borehole (Slurry unit weight)

Moment of inertia of pipe wall cross
section

Pipe ring deflection to buoyant force
ASTM F 1962 (Eq. X2.6, p.6)

D2.1 Buoyant Deflection (Long Term)

Please note that long term buoyant deflection was assumed negligible, since grout is assumed to be cured after a 1-week period from installation/pumping.

D3 - Reissner Effect Deflection (Short Term)

D3.1 - Reissner Effect Deflection (Short Term)

$$\mu_{short} := 0.35$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{short}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.0000033$$

Poisson's Ratio for PE pipe material at
short term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{short}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect

D3.2 - Reissner Effect Deflection (Long Term)

$$\mu_{long} := 0.45$$

$$R = 1000 \text{ ft}$$

$$z := \frac{\frac{3}{2} \cdot (1 - \mu_{long}^2) (D_1 - t)^4}{16 \cdot t^2 \cdot R^2} = 0.000003$$

Poisson's Ratio for PE pipe material at
long term (ASTM F 1962, 8.2.4.2)

Radius of curvature

Deflection due to longitudinal bending

$$\Delta y_{R_{long}} := \left(\frac{2}{3}\right) \cdot z + \left(\frac{71}{135}\right) \cdot z^2 = 0.0002\%$$

Pipe ring deflection due to the Reissner
Effect, long term

D4 - Net Ring Deflection

$$\Delta y_{lim} := 7.5\%$$

Deflection limit for DR 9 non pressurized pipe (Table 2 , p. 437, PPI Handbook)

D4.1 - Net Short Term

$$\Delta y_{short_net} := \Delta y_{ELD_short} + \Delta y_{bouyant} + \Delta y_{R_short} = 0.3\% \quad \text{Percent ring deflection in short term analysis}$$

$$Check := \text{if}(\Delta y_{short_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D4.2 - Net Long Term

$$\Delta y_{long_net} := \Delta y_{ELD_long} + \Delta y_{R_long} = 0.5\% \quad \text{Percent ring deflection in long term analysis (50 years)}$$

$$Check := \text{if}(\Delta y_{long_net} < \Delta y_{lim}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5 - Unconstrained Ring Buckling

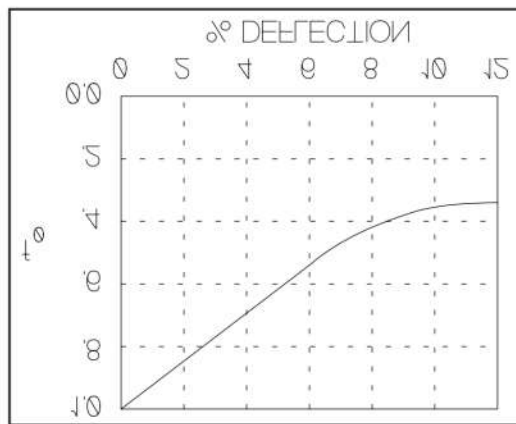
D5.1 - Unconstrained Ring Buckling, Levy's Equation (Short Term-During Pull)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{short} := 0.35$$

$$E_{short} = 57500 \text{ psi}$$



Factor of Safety

Poisson's Ratio for PE pipe material at short term (ASTM F 1962, 8.2.4.2)

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 10 hrs of sustained loading (Table X1.1 ASTM F 1962)

Ovality compensation factor, Figure 3 (PPI Chp. 12). Calculated deflection limit in section D4.1

$$f_{o_short} := 0.99$$

$$P_{UC_short} := \left(\frac{2 \cdot E_{short}}{1 - \mu_{short}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_short}}{N} = 126.7 \text{ psi} \quad \text{Allowable unconstrained buckling pressure}$$

$$H = 46 \text{ ft}$$

Elevation difference between the lowest point in borehole and entry or exit pit

$$P_{mud} := \gamma_m \cdot H = 22.36 \text{ psi}$$

Pressure of drilling slurry

$$P_{net} := P_{mud} = 22.36 \text{ psi}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_short} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

D5.2 - Unconstrained Ring Buckling, Levy's Equation (Long Term)

Note that constraining the pipe will increase the pipe's buckling strength, therefore considering an unconstrained condition will produce a conservative value.

$$N := 2.0$$

$$\mu_{long} := 0.45$$

Factor of Safety

Poisson's Ratio for PE pipe material, long term (ASTM F 1962, 8.2.4.2)

$$E_{long} = 28200 \text{ psi}$$

Apparent modulus of elasticity for PE4710, Base Temperature of 73 deg. Fahrenheit at 50 years of sustained loading (Table X1.1 ASTM F 1962)

$$f_{o_long} := 0.9$$

Ovality compensation factor, Figure 3 (PPI Chp. 12). Use deflection limit calculated in Section D4.2

$$P_{UC_long} := \left(\frac{2 \cdot E_{long}}{1 - \mu_{long}^2} \right) \cdot \left(\frac{1}{DR_1 - 1} \right)^3 \cdot \frac{f_{o_long}}{N} = 62.2 \text{ psi}$$

Allowable unconstrained buckling pressure

$$P_{GW} := \gamma_w \cdot H_w = 0 \text{ psi}$$

Groundwater head pressure

$$P_{net} := P_{GW}$$

Net external loading with open borehole

$$Check := \text{if}(P_{UC_long} > P_{net}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

References

1. ASTM F 1962 -05 Use of Maxi-Horizontal Directional Drilling for Placement of Polyethylene Pipe or Conduit Under Obstacles, Including River Crossings
2. ASTM F 1804-08 Standard Practice for Determining Allowable Tensile Load for Polyethylene (PE) Gas Pipe During Pull-In Installation
3. Proposed Soil Properties for CHPE Package 1 HDDs, Kiewit, October 12, 2022.
4. Handbook of Polyethylene Pipe, 2008, Plastics Pipe Institute (PPI), Second Edition
5. Larry Slavin, 2009, Guidelines for Use of Mini-Horizontal Direction Drilling for Placement of High Density Polyethylene Pipe
6. Mohammad Najafi, 2013, Trenchless Technology, First Edition, McGraw Hill

96.XX

Defining Parameters of Horizontal Directional Drilling :

$D_1 := 10.75 \text{ in}$	Pipe 1 outer diameter
$D_2 := 2.375 \text{ in}$	Pipe 2 outer diameter
$D_{rod} := 3.5 \text{ in}$	Assumed drill rod diameter
$DR_1 := 9$	Dimension ratio of Pipe 1
$DR_2 := 11$	Dimension ratio of Pipe 2
$T_{p1} := \frac{D_1}{DR_1} = 1.194 \text{ in}$	Thickness of Pipe 1
$T_{p2} := \frac{D_2}{DR_2} = 0.216 \text{ in}$	Thickness of Pipe 2
$C_1 := \pi \cdot D_1 = 33.8 \text{ in}$	Pipe circumference of pipe 1
$C_2 := \pi \cdot D_2 = 7.5 \text{ in}$	Pipe circumference of pipe 2

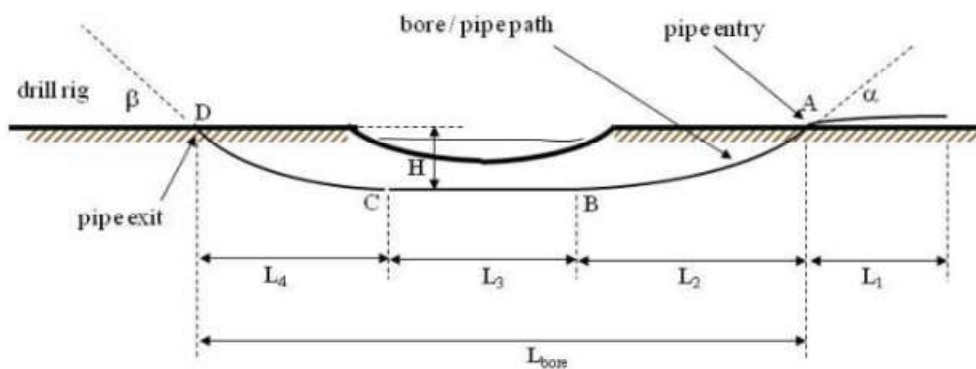


Illustration 1 - Schematic of Drive Cross-section

$\alpha := 12^\circ$	$\alpha_{in} := \alpha = 0.2094 \text{ rad}$	Borehole entry angle (degrees, radians)
$\beta := 8^\circ$	$\beta_{exit} := \beta = 0.1396 \text{ rad}$	Borehole exit angle (degrees, radians)
$D_r := 18 \cdot \text{in}$		Final reamed bore diameter
$H_{max} := 79.8 \text{ ft}$		Max depth of bore hole to final reamed bore diameter
$H_{max1} := H_{max} + \frac{D_r}{2} = 80.55 \text{ ft}$		Max depth to bore hole springline from ground surface
$L_{total} := 2124.6 \text{ ft}$		Total length of HDD crossing
$L_1 := 150 \text{ ft}$		Assumed pipe drag on surface, See Illustration 1
$L_2 := 208.2 \text{ ft}$		Horizontal length to achieve depth - provided by Contractor, See Illustration 1
$L_3 := 1609 \text{ ft}$		Straight horizontal section
$L_4 := 307.4 \text{ ft}$		Horizontal distance to rise to surface, See Illustration 1
$H := 16.8 \text{ ft}$		Elevation difference between the lowest point in borehole and slurry pump elevation (entry or exit pit), See Illustration 1

$$v_a := 0.1$$

Friction coefficient before pipe enters
(rollers assumed)

$$v_b := 0.3$$

Friction coefficient for the bundle within
borehole (lubrication assumed)

$$\rho_w := 62.4 \text{ pcf}$$

Unit weight of water

$$\gamma_a := 0.965$$

Specific gravity of pipe

$$\gamma_m := 90 \text{ pcf}$$

Assumed unit weight of slurry

$$\gamma_b := \frac{\gamma_m}{\rho_w} = 1.4$$

Specific gravity of slurry, assumed unit
weight

$$\gamma_c := 1.0$$

Specific gravity of water to fill the pipe

$$\Delta P := 10 \text{ psi}$$

Hydrokinetic Pressure (p. 443, Ch12 PPI
Handbook)

$$g := 32.2 \frac{\text{ft}}{\text{s}^2}$$

Gravitational Constant

A - Axial Bending Stress:

$$R_{avg_in} := 1000 \text{ ft}$$

Radius of curvature at the entry, provided
by Contractor

$$R_{avg_out} := 1000 \text{ ft}$$

Radius of curvature at the exit, provided
by Contractor

$$R := \frac{R_{avg_in} + R_{avg_out}}{2} = 1000 \text{ ft}$$

Average radius of curvature at entry

$$r_{rod} := 1200 \cdot D_{rod} = 350 \text{ ft}$$

ASTM F 1962-99, Equation 1, p7

$$Check := \text{if}(R_{avg_in} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

$$Check := \text{if}(R_{avg_out} > r_{rod}, \text{"okay"}, \text{"not okay"}) = \text{"okay"}$$

Radius of curvature should exceed 40 times the pipe outside diameter to prevent ring collapse.

$$e_a := \frac{D_1}{2 \cdot R} = 0.0004$$

Strain within the casing pipe

$$E_{12hr} := 57500 \cdot \text{psi}$$

Apparent modulus of elasticity for PE4710,
Base Temperature of 73 deg. Fahrenheit at
10 hrs of sustained loading (Table X1.1
ASTM F 1962)

$$S_a := e_a \cdot E_{12hr} = 25.8 \text{ psi}$$

Axial bending stress within the casing pipe

B - Site Specific Analyses: Pullback Force:

B1 - Empty Pipe

B1.1 - Effective Weight of Empty Pipe:

$$w_a := \frac{\pi}{4} \left((D_1^2 - (D_1 - T_{p1})^2) + (D_2^2 - (D_2 - T_{p2})^2) \right) \cdot \rho_w \cdot \gamma_a = 8.3 \text{ plf}$$

B1.2 - Upward Buoyant Force:

Effective weight

$$w_b := \left(\frac{\pi \cdot (D_1^2 + D_2^2)}{4} \right) \rho_w \cdot \gamma_b - w_a = 51.2 \text{ plf} \quad \text{Upward buoyant force of empty pipe}$$

B1.3 - Hydrokinetic Pressure:

$$\Delta T := \Delta P \cdot \left(\frac{\pi}{8} \right) (D_r^2 - (D_1^2 + D_2^2)) = 796 \text{ lbf} \quad \text{Hydrokinetic force}$$

B1.4 - Pullback Force Point A:

$$T_a := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1925 \text{ lbf}$$

Pullback force when pipe enters the ground

B1.5 - Pullback Force Point B:

$$T_b := e^{v_b \cdot \alpha_{in}} (T_a + v_b \cdot |w_b| \cdot L_2 + w_b \cdot H_{max} - v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 9619 \text{ lbf}$$

Pullback force increase with depth

B1.6 - Pullback Force Point C:

$$T_c := T_b + (v_b \cdot w_b \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 32888 \text{ lbf}$$

B1.7 - Pullback Force at D:

$$T_d := e^{(v_b \cdot \beta_{crit})} \cdot (T_c + v_b \cdot |w_b| \cdot L_4 - w_b \cdot H_{max} - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 34681 \text{ lbf}$$

B1.8 - Maximum Pullback Force - Empty Pipe:

$$P_{max_empty} := \max(T_a, T_b, T_c, T_d) + \Delta T = 35477 \text{ lbf}$$

Maximum Pullback Force

B2 - Filled Pipe with Water

B2.1 - Upward Buoyant Force:

$$w_{b\text{filled}} := \left(\frac{\pi \cdot D_1^2}{4} \right) \cdot \rho_w \cdot \left(\gamma_b - \gamma_c \cdot \left(1 - \left(\frac{2}{DR_1} \right)^2 \right) \right) - w_a = 24.6 \text{ plf}$$

Upward buoyant force of pipe filled with water

B2.2 - Pullback Force Point A:

$$T_{a\text{filled}} := e^{v_a \cdot \alpha_{in}} \cdot (v_a \cdot w_a \cdot (L_1 + L_2 + L_3 + L_4)) = 1925 \text{ lbf} \quad \text{Pullback force enter ground}$$

B2.3 - Pullback Force Point B:

$$T_{bfilled} := e^{v_b \cdot \alpha_{in}} (T_{afilled} + v_b \cdot |w_{bfilled}| \cdot L_2 + w_{bfilled} \cdot H_{max} + v_a \cdot w_a \cdot L_2 \cdot e^{(v_a \cdot \alpha_{in})}) = 5971 \text{ lbf}$$

Pullback force increase and decrease with depth

B2.4 - Pullback Force Point C:

$$T_{cfilled} := T_{bfilled} + (v_b \cdot |w_{bfilled}| \cdot L_3) - e^{(v_b \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_3 \cdot e^{(v_a \cdot \alpha_{in})}) = 16418 \text{ lbf}$$

B2.5 - Pullback Force at D:

$$T_{dfilled} := e^{(v_b \cdot \beta_{exit})} \cdot (T_{cfilled} + v_b \cdot |w_{bfilled}| \cdot L_4 - e^{(v_a \cdot \alpha_{in})} \cdot (v_a \cdot w_a \cdot L_4 \cdot e^{(v_a \cdot \alpha_{in})})) = 19214 \text{ lbf}$$

B2.6 - Maximum Pullback Force - Filled Pipe with Water:

$$P_{max} := \max(T_{afilled}, T_{bfilled}, T_{cfilled}, T_{dfilled}) = 19214 \text{ lbf}$$

Maximum Pullback Force

B3 - Safe Pull Strength / Ultimate Tensile Load Check:

B3.1 Safe Pullback Check

$$A_1 := \frac{\pi}{4} (D_1^2 - (D_1 - T_{p1})^2) = 19 \text{ in}^2$$

Cross-sectional area of Pipe 1

$$A_2 := \frac{\pi}{4} (D_2^2 - (D_2 - T_{p2})^2) = 0.8 \text{ in}^2$$

Cross-sectional area of Pipe 2

$$P_{11} := \frac{A_1 \cdot P_{max_empty}}{A_1 + A_2} = 34101 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Empty)

$$P_{21} := \frac{A_2 \cdot P_{max_empty}}{A_1 + A_2} = 1376 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Empty)

$$P_{12} := \frac{A_1 \cdot P_{max}}{A_1 + A_2} = 18468 \text{ lbf}$$

Pullback forces acting on Pipe 1 (Ballast)

$$P_{22} := \frac{A_2 \cdot P_{max}}{A_1 + A_2} = 745 \text{ lbf}$$

Pullback forces acting on Pipe 2 (Ballast)

$$P_{SPF1} := 41214 \text{ lbf}$$

Safe pullback forces Pipe 1 (Table %, p. 448, PPI)

$$P_{SPF2} := 1683 \text{ lbf}$$

Safe pullback forces Pipe 2 (Table %, p. 448, PPI)

check := if ($P_{SPF1} > P_{11}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{21}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF1} > P_{12}$, "okay", "not okay") = "okay"
 check := if ($P_{SPF2} > P_{22}$, "okay", "not okay") = "okay"